# EB MEASURING TRAVEL TIME RELIABILITY VARIABLES IN A NON-SIGNAL HIGHWAY TRAFFIC ROUTE

Musa Adamu Eya<sup>1</sup>\*, Gobi Krishna Sinniah<sup>2</sup>, Muhammad Zaly Shah<sup>3</sup>, Abdullahi Hashim<sup>4</sup>.

<sup>1</sup> Department of Transportation Planning <sup>2, 4</sup> Department of Urban and Regional Planning, Faculty of Built Environment and Surveying <sup>3</sup>Centre for Innovative Planning and Development (CIPD), Faculty of Built Environment and Surveying UNIVERSITI TEKNOLOGI MALAYSIA

# Abstract

Traffic congestion has become a severe scourge in highly densely populated towns in both developed and developing countries. Longer travel times, as well as a higher incidence of crushed vehicles, environmental issues, and deterioration in the quality of life, have been caused by increased demand for urban mobility and transit. Highway traffic congestion is often considered a routine occurrence; plan period accordingly. The study looks into the measure variables that influence travel time reliability (TTR). However, severe and unanticipated delays disrupted deliveries, program, and activity schedules, operations, and other logistics. In other words, the study looks into the potential factors that influence travel time reliability (TTR). This study used the Highway Capacity Manual (HCM) as a basis to assess the travel time reliability index. The study employed Log odd ratio to identify the relationship between the Buffer Time Index (BTI) and the planning time index (PTI) and determine the travel time-reliability threshold ratio, and the Planning Time Index (PTI) and also, determine the ratio of the travel time-reliability threshold. The study revealed the following: the diversion of 15%–20% of the total traffic from the high-level congested roads to the results of the least or lesser congested roads into a higher level of service (lower congestion), an increase in speed by 15km/h to 20km/h from the current speed levels, and increases by 10%–15%, respectively. The study indicates no relationship between traffic flow and travel time. The study also provides a better understanding of the system's capabilities, limitations, and data collection for real-time performance measurement.

*Keywords:* Travel time, Reliability, Buffer time index, Planning time index, Highway Capacity Manual.

Doctor of Philosophy at Universiti Teknologi Malaysia. Email: musaeya@graduate.utm.my

# **1.1.Introduction**

Building variables for the effective performance of corridor highway travel times is critical for transportation planners and highway engineers who specialise in road design. Travel

time variables have become a critical and essential facet of transportation accomplishments. They can be treated as effectual elements of travel time, reliability, and execution.

They correspond to the efficiency of highway travel time, which may have an easily understood meaning when travelling with others. Flow, along with other variables such as speed, volume, flow, time, density, traffic incidence, work zone, and weather, form important attributes of travel time reliability. Travel time depends on these variables for efficient and effective travel from the origin to a destination. The travel time reliability model is dependent on volume and density. Volume and density will be considered the main variables for assessment. The method to quantify travel time reliability metrics can be grouped into variation metrics, probabilistic measures, and percentile indices (Kidando et al., 2019).

Traffic flow and volume are very important components that estimate the rate of traffic passing on a road segment at a particular time interval. The flow rate could be minute, hours, day, week, month, and year. Volume is the sum of vehicles flying road at a time interval less than or within an hour.

Various measures, such as level of service, delay, buffer size, and volume capacity ratio, are used to measure travel time reliability (TTR) as key initiatives for the efficiency of vehicular traffic on the explicit road system (Kidando et al., 2019). Travel time can be viewed in two ways: the running time and the intersection delay. The former defined a function of link length, which is dependent on highway geometry design capacity; the latter provides a reliable forecast of intersection delay time prediction performance (Lu et al., 2021)(Otuoze et al., 2021).

Network reliability is the load quantity of connected travel time reliability (Kathuria et al., 2017)(Kathuria et al., 2020). Travel time variability was defined by (Bimpou & Ferguson, 2020) as the distinction between an upper and lower range expressed in terms of travel time percentiles. (Nicholson, 2003) identifies how the effects of disruption lie on the hierarchy of understanding the transport network acquired by the users. Microsimulation may best fit the modelling strategies for assessing the effects of short-term disruption.

Network reliability is the load quantity of connected travel time reliability (Wang & Guo, 2022). It is the accumulated time for the journey from one location to another(Khoo et al., 2021) encoded by the functional consistency of a particular road segment. Travel time reliability is the temporal variability of travel time that influences many aspects of travel decisions, particularly in roadway transportation (Afandizadeh Zargari et al., 2021). The discrepancy in travel time that is not anticipated by motorists is referred to as "travel time reliability"(Texas Transportation Institute & Cambridge Systems, 2006). Travel time can be defined as the amount of time it takes a vehicle to complete a specified trip over a segment of road between two points.

Travel Time Reliability describes the consistency of travel times from day to day or across distinct intervals of the day (FHWA, 2019)(Transportation Research Board, 2010)(Zheng et al., 2018)(Kong et al., 2018)(Olszewski et al., 2018)(H. Li et al., 2019)(E. O. A. Tufuor & Rilett, 2020)(E. Tufuor et al., 2021)(E. O. A. Tufuor & Rilett, 2020)(E. Tufuor et al., 2021)(E. O. A. Tufuor & Rilett, 2021)(Bimpou & Ferguson, 2020)(Siddiqui & Ko, 2020)(Wu et al., 2022)(Steinmaßl et al., 2021)(Rivera-Royero et al., 2022)(No & For, 2022)(Chung et al., 2020). The Travel Time Index (TTI) is the ratio of average travel time and free-flow or

speed-limit (Chung et al., 2020). Travel Time Index is defined as the ratio of mean travel time to free-flow travel time (Federal Highway Administration, 1991)(Roess et al., 2010)(Transportation Research Board, 2010)(FHWA, 2019)(E. O. A. Tufuor & Rilett, 2020)(Wu et al., 2022).

Travel time estimation and forecasting assist transportation operators in initiating better monitoring and coordination of an efficient signal control system, as well as allowing travellers to plan informed journeys based on road selection and take-off time (Lu et al., 2021). Travel time reliability can be estimated endogenously, and changes in the values. Forecasting mass transit travel times is an effective measure for improving service reliability, optimising travel orders, and mitigating traffic challenges (Zhang et al., 2022).

### **1.2. Background of the Study**

Travel time variables are an important aspect of transportation planning, and highway engineers evaluate unchangeable factors that influence a specific trip. These variables are so significant in this research because they are the ingredients that attach a high value to reliability assessment. These variables serve as a major attribute that defines the changeability of route dependency, without understanding these variables, trip makers may not adequately understand the success and failure of a particular journey. Traffic volume may tend to maintain or reach an equilibrium position when speed increases, and travellers may face delays when the speed reduces. As a result, peak-period trips increase until a certain time of day and limit further flow.

Density affects vehicular movement when the flow and traffic volume exceed the road capacity; which may result in high-density traffic. It may reduce the traveller's benefit from road capacity to accommodate the number of vehicles moving in a particular lane. The variables may influence trip planners because most travellers are willing to forego time wasted on a particular journey. This study aimed to identify the variable used in measuring corridor highway travel time reliability in Nigeria. The following objectives are focused on: First, identify the variables used in measuring corridor highway travel time. Secondly, assess the effectiveness of travel time variables. Thirdly, the relationship between each variable and expected values.

# 2.0. Literature Review

# 2.1. Literature Review

Traffic congestion prediction is crucial for strengthening the energy success and reliability of the transportation system (Shelke et al., 2022). Travellers make decisions about which roads to take and when to leave based on the anticipated travel time and their reliability (Zheng et al., 2018); (Khoo et al., 2021). Determining the performance of management measures related to highway system reliability, freight, and traffic composition can be assessed in accordance with FHA standards (Siddiqui & Ko, 2020) Unreliability could be caused by endogenous and exogenous factors such as demand variation, incidents, weather, special events, system malfunctions, and the performance of supplementary and competing transportation modes (Z. Chen et al., 2019). The investigations into travel time reliability include the potential transit satisfaction of smart mobility technology in a mixed highway traffic construction zone (Abdulsattar et al.,

2020). Car ownership has generated an enormous concentration of automobiles on the road network in modern cities (Hameed et al., 2019; Tsuboi, 2021).

The presence of heavy and sluggish vehicles in the traffic stream reduces traffic capacity significantly for the flow of moving passenger automobiles (Macioszek, 2019). Road infrastructure, unregulated road conditions, informal activities, off-street parking, and insufficient public transportation were the significant reasons for traffic congestion on the Abuja-Kugbo-Nyaya axis (Chidera, 2020). To establish a congestion travel time reliability threshold, the study will evaluate measures of corridor highway traffic with travel time reliability to disaggregate traffic flow and travel time index using buffer time index (BTI) and planning time index (PTI). In the event of congestion, reliability is measured by the buffer time index and standard deviations from the foreseeable traffic flow connected with a given traffic situation. The study anticipates travel time reliability as a dependent variable for calculating the Highway Capacity Manual's Buffer Time Index (BTI) and Planning Time Index (PTI).

### 2.2. Traffic Flow Theories, and Travel Time Models

Travel time reliability measures have gained widespread attention in transportation planning and engineering for a couple of years. (Becker, 1965) believes that the budgeting and effectiveness of the no-working period are more important to economic welfare than other working times. According to (Becker, 1965) consumer goods are those that openly promote satisfaction. Gaver proposed a travel time model and predict variability in travel time (Gaver, 1968). Comparing alternative models, it is variations in system reliability tendencies that are more of a concern (Aven, 1988).

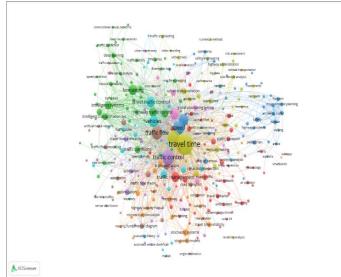
Knight developed commuter response data to estimate a "safety margin" (Knight, 1974) Small conducted an experimental and verifiable study on this topic and discovered that the timing of travellers' departures is greatly influenced by plan costs (Arnott & Small, 1994) (D'Este et al., 1999) proposed a game theory to measure the performance of reliability in transport networks to predict the trade-off between users exploring a route to reduce the foreseeable journey cost and selecting a link performance situation to optimise the foreseeable journey cost. Noland and Small used this theory to explain how travel time and departure time relate to different congestion rates. Travel time can be categorised into performance-driven and reliability measures and traveller's response to reliability. Lomax et al. were among the old scholars who studied travel time reliability measures that demonstrate a practical performance (Lomax et al., 2003). The Burr distribution is elastic and easy to apply as a failure-time model.

The Burr has a good estimation of the Weibull, which is a restricted distribution of the Burr (Zimmer et al., 1998). The authors established an alternative statistical distribution for TT variability, with the Burr Type XII distribution scoring the highest value and being more applicable for both links and roads (Susilawati et al., 2010)(Taylor & Susilawati, 2012). (Nicholson, 2003) suggested that unreliability be accepted as a step up from two. The Burr has a good estimation of the Weibull, which has a restricted distribution (Zimmer et al., 1998). The effectiveness of travel time reliability variables is a

matter of deciding on departure time, and this research is associated with the relevant theory of variability developed in the context of the transportation field. Studying the current state of reliability data requires a rigorous understanding of the variable measures and the means by which appropriate findings can be made that will contribute to highway travel time reliability.

Reliability demonstrates the concept of recurrence, though it is open to interpretation. A person making a single trip may want to know that the trip time is uncertain, and this must be considered even if the journey is never to be repeated. There is an implicit assumption that if it was recurring. The results and, in some cases, the designated travel time may differ. As a result, reliability is closely related to the statistical concept of variability. Kathuria et al., (2017) demonstrated that speed, density, and volume can be used to estimate travel time reliability (TTR) as well as be viewed as a performance of travel time variability (TTV). (Kathuria et al., 2020) further presented another measure of planning time as the 95<sup>th</sup> percentile of travel time, meaning how bad a vehicle travel time delay can be. (Samal et al., 2020) used a video graphic mobile camera to estimate traffic volume.

Nnamani et al., (2020) video graphics survey method using a probe vehicle approach. The authors provide the following traffic congestion measures, which include speed, travel time, delay, and level of service (Afrin & Yodo, 2020). Different metrics, probability measures, and percentile ratios can be used to quantify TTR (Kidando et al., 2019). The variable that contributes to the traffic congestion unit of measure can be considered reliable if the volume of traffic remains constant throughout the evaluation (Siddiqui & Ko, 2020). The BTI, according to Hongtai Yang et al. (2020) can be calculated using a regression model to estimate percentile rank and standard error.



<u>Analysis</u>

-Total number of clustered = 8 -Total number of cooccurrence

Layout Parameters

-Random = 1 -Max, Iteration = 1000 -Initial Stepsize = 1.000 -Stepsize Reduction = 0.75 -Stepsize Convergence = 0.001 Random Seed = 0

Figure 1. Authors Bibliometric Analysis on traffic flow and travel time

# 2.3. Metric Analysis

# Analysis

• Total number of clustered = 8

• Total number of co-occurrence

### Layout Parameters

- Random = 1
- Max, Iteration = 1000
- Initial Stepsize = 1.000
- Stepsize Reduction = 0.75
- Stepsize Convergence = 0.001
- Random Seed = 0

# 2.4. Method of Estimating Travel Time Index.

The researchers adopt two critical measures which include the ratio of congestion level to traffic congestion and the ratio of travel time reliability (Kong et al., 2018). Travel Time Index – TTIR (travel time index ratio). TTI will be used to measure congestion intensity. The common TTI defines the average TT divided by the free-flow TT.

| S/NO. | TT Measures         | Definition  | Relevance  |
|-------|---------------------|---|--|
| 1     | PTI                 | 90 <sup>th</sup> /95 <sup>th</sup> Percentile<br>FFT        | Personal trip & urban<br>trip                      |
| 2     | BTI                 | <u>95<sup>th</sup> Percentile – T<sub>avg</sub>.</u><br>FFT | <i>Commercial trip, logistic service, carriers</i> |
| 3     | TTI                 | $rac{T_{avg}}{FFT}$  | Used as a congestion measure                       |
| 4     | Misery Index        | <u>5% worst Tavg</u><br>FFT                                 | Used as an instrument to estimate bad trips        |
| 5     | J Skew              | <u>5% worst Tavg.</u><br>FFT                                | Operator Side Index                                |
| 6     | ג variance          | <u>TT90 - TT 10</u><br>TT50                                 | Operator Side Index                                |
| 7     | $P(T_{ave} + ATTV)$ | Percentile when TT is ATT above T <sub>ave</sub>            | User Side Index                                    |
| 8     | $P(T_{ave} - DTTR)$ | Percentile when TT is ATT above $T_{ave}$                   | User Side Index                                    |
| 9     | TT80 - TT20         | -   | Range of average TT                                |
| 10    | <i>TT70 – TT30</i>  | -   | Range of average TT                                |

Table 1. Travel Time Reliability Measures

Source: Adapted from Jose and Ram., 2019

# 2.4.1. Planning Time Index (PTI)

*The planning time index measures the dependability of travel time. It is calculated by dividing the 95th percentile by the smooth flow journey time.* 

 $PTI = rac{95th \ percentile \ of \ travel \ time \ of \ all \ observations \ during \ one \ hour \ of \ the \ selected \ route}{free \ flow \ travel \ time \ of \ route}$ 

 $TTI = \frac{95th \ percentile \ travel \ time \ of \ point \ A/free \ flow \ travel \ time \ of \ route \ A}{95th \ percentile \ travel \ time \ of \ route \ B} flow \ travel \ time \ of \ route \ B}$ 

 $TTI = \frac{95th \ percentile \ speed \ of \ point \ A * free \ flow \ travel \ time \ of \ route \ B}{95th \ percentile \ of \ travel \ time \ of \ route \ B * free \ flow \ travel \ time \ of \ route \ A}$ 

#### 2.4.2. Buffer Time Index (BTI)

Travel Time Index (Chung et al., 2020)

$$TT_{mean} = \frac{TT_{95th-Average Travel Timme}}{Average Travel Time} \times 100 (\%)$$

$$BI_{median} = \frac{TT_{95th-Median Travel Timme}}{Average Travel Time} \times 100 (\%)$$

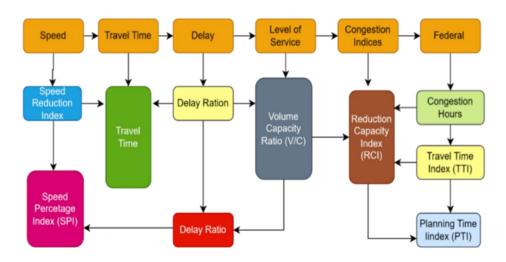
$$PI = \frac{TT_{95th}}{TT_{free flow or pasted speed limit}}$$

$$BTI = \frac{T_{95-T_{50}}}{T_{50}} = \frac{T_{95}}{T_{50}} - 1$$

### Table 2. Reliability Performance Measures

| Reliability                       | Definition   | Unit       |
|-----------------------------------|--|------------|
| <b>Performance metrics</b>        |  |            |
| Planning Time Index               | 90 <sup>th</sup> percentile travel time index (90 <sup>th</sup> percentile travel time divided by the free flow travel time) | None       |
| Buffer Index                      | Is the 95 <sup>th</sup> travel time minus the average normal travel time   | Percentile |
| Failure/On-Time                   | Percentile travel times multiply by median travel time.  | Percentile |
| Measures                          | Measures, 45 mph; and 30 mph   |            |
| 8 <sup>th</sup> Percentile Travel | 80 <sup>th</sup> percentile travel time divided by the free flow travel time   | None       |
| Time Index                        | th   |            |
| Skew Statistic                    | (90 <sup>th</sup> percentile minus the median) travel time)  | None       |
| Misery Index                      | The average travel time divide Skew Statistics by the free flow travel time  | None       |

Source: Adapted from ("Inc. Reliab. Perform. Meas. into Transp. Plan. Program. Process.," 2013).



### Figure 2 Reliability Measures: (Afrin & Yodo, 2020).

Table 3. Different Author's Reviewed Variables for measuring Travel Time Reliability

| S/No | Author's           | Identified variables                | Outcome                                      |
|------|--------------------|-------------------------------------|--|
| 1    | (S. Li et al.,     | Volume, density map                 | Time Spatial Net outperforms the tested      |
|      | 2022)              |                                     | representation of variables                  |
| 2    | (Tsuboi, 2021)     | Traffic volume, vehicle speed       | Traffic flow proved better                   |
| 3    | (E. O. A.          | The incident, work zone, and        | Suitable for assessing TTR for a large       |
|      | Tufuor &           | weather                             | corridor and network in a single run.        |
|      | Rilett, 2021)      |                                     |  |
| 4    | (Z. Chen &         | Time of day, day of week, and       | Travel time ahead 15 minutes contribute      |
|      | Fan, 2021)         | weather                             | the most forecasted travel time              |
| 6    | (Romanowska        | Average speed, flow, and density    | The model used does not provide good         |
|      | & Jamroz,          |                                     | results for the variables, and suggested for |
| _    | 2021)              |                                     | standard deviation                           |
| 7    | (Nnamani et        | Traffic volume, speed of a          | Highly significant                           |
| 0    | al., 2020)         | vehicle, density, and traffic flow. |  |
| 8    | (Afrin & Yodo,     | Speed, travel time, delay, and      | Applied a non-probabilistic technique.       |
|      | 2020)              | level of service                    | Future studies should employ probabilistic   |
| 10   | (1.1               | X7.1                                | measures in assessing the variables          |
| 10   | (Jabari et al.,    | Volume, density, and speed          | Inadequate information about the number      |
| 11   | 2019)<br>(Maghrour | Flow, speed, and density.           | of vehicles in the system is expected        |
| 11   | Zefreh &           | Flow, speed, and density.           | Lognormal is mostly fitted with variables.   |
|      | Török, 2020)       |                                     |  |
| 12   | (Ibarra-           | Filter (speed), assignment, Fill,   | GPS Mean & standard deviation values are     |
| 12   | Espinosa et al.,   | traffic flow, & aggregation using   | mostly fitted                                |
|      | 2019)              | mean & STD.                         | mostry meet                                  |
| 13   | (Kidando et al.,   | TTR, TV(AADT), truck volume,        | Bayesian & multi-logistic proved same        |
|      | 2019)              | landuse, speed, road condition,     | though, Bayesian performance better.         |
|      | /                  | lanes, road function, segment       |  |
| 12   | (P. Chen et al.,   | Time, and road types                | Future studies should adopt larger-scale     |
|      | 2018)              | **                                  | probe data in the time frame.                |
| 14   | (Fulari et al.,    | Flow, and density                   | The method was highly fitted in evaluating   |
|      | 2019)              | -                                   | error and can be used in computing density   |
| C    | Author Davian      | 0000                                |  |

Source: Author Review 2022.

### 2.4.3. Variable Use in Assessing Travel Time

- **a. Speed:** Is the distance covered (traveled) per unit of time that is how fast a vehicle is moving. It is also the time rate at which a vehicle is moving along the road.
- **b.** Volume: Is the comprises all modes of vehicles fly at a segment or lane during a specific time interval.
- **c. Density:** Is the total number of vehicles count per lane per freeway (highway) length in miles or kilometres.
- **d.** Flow: Is the movement of individual vehicle between two location and interchange with each other. That is the total number of vehicles passing a road at both entry and exit

e. Time: Is the measure of sequence of events. It is the dimension on event that take place

# **3.1. Methodology and Data Description**

The traffic survey was conducted at Masaka, and Ado along Abuja road, which is a four-lane road. The traffic volume was daily traffic based on hourly traffic count data. The survey data was used to determine the percentage change traffic flow for the morning hours and that of the evening period. The percentage change was applied to the travel for a complete day to obtained an estimated flow and travel time or delay time at the traffic spots. The study recorded both entry and exit traffic. The study employed a smartphone to record traffic data every minute. The techniques are easy to transfer to an external storage device.

The video camera was used to collect traffic data at an interval of one hour. The recorded data was compared with manual counting for accuracy. The study employed passenger car unit (PCU) values to determine the various modes of transport, and the average traffic density for the time period (6:00 a.m. to 6:00 p.m.).

# **3.1.2 Research Framework**

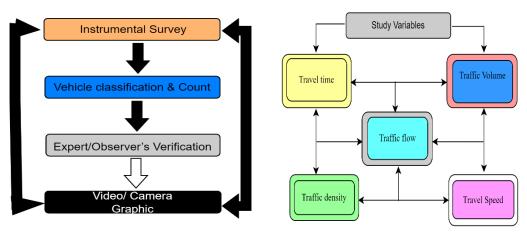


Figure 3. Process of Data Collections

Figure 4. Study Variables

Table 4. Roads Designs and Capacity Volume.

| S/No. | Type of carriageway        | Design service | e for different categorie | s of urban road |
|-------|----------------------------|----------------|---------------------------|-----------------|
|       |                            | Arterial *     | Sub-arterial **           | Collector ***   |
| 1     | 2 lanes (1 way)            | 2400           | 1900                      | 1400            |
| 2     | 2 lanes (2 way)            | 1500           | 1200                      | 900             |
| 3     | 3 lane 91 way0             | 3600           | 2900                      | 2200            |
| 4     | 4 lanes undivided (2 way)  | 3600           | 2400                      | 1800            |
| 5     | 4 lanes divided (2 way)    | 3600           | 2400                      | -               |
| 6     | 6 lanes undivided 92 (way) | 4800           | 3800                      | -               |
| 7     | 6 lanes divided (2 way)    | 5400           | 4300                      | -               |
| 8     | 8 lanes divided 2 (way)    | 7200           | -                         | -               |

Adapted from (Indian Roads Congress, 1990)

- \* Road with no frontage access, no standing vehicle cross traffic
- \* \*\* Roads with frontage access but no standing vehicles and high-capacity intersection
- \* \*\*\* Road with free frontage access, parked and heavy cross traffic

### 3.2. The Highway Capacity Manual (HCM6) Travel Time Reliability.

The HCM6 measure developed a strategy to model variables such as work zones, snow-rain weather, special events, incidents, demand differences, and hybrid systems. The target of the HCM6 principle is to provide a quality source of variability when calculating the travel time distribution (probability). The assessment covered a period of one year. This is considered the reliability report based on the HCM analysis of travel time distribution. The study selected a 1-hour interval aggregate for data analysis.

# **3.2.1.** Congestion Index

$$CI = \frac{TT}{TTN}$$

$$CI = f(x1 \ x2 \ x3) + f(HA)$$

$$CI = \frac{C - C_0}{C_0}$$

Where: C = Actual travel time,  $C_0 = Free flow time$ 

CI near/close to zero meaning very low level of congestion.

CI > 2 meaning severely congested condition.

Travel Time Ratio

$$TTR = \frac{CTR}{FFTR}$$

Congestion time rate

$$CTR = \frac{TT}{D}$$

Delay Time rate

DTR = 
$$\frac{DR}{CTR}$$
  
Speed:  $\mathbf{V} = \frac{d}{t}$   
Time:  $\mathbf{T} = \frac{d}{s}$ 

**Distance:** S = s \* t

### 3.2.2. Standard Deviation and Variance

$$SD = \sqrt{\sum \frac{(x - \overline{x})^2}{n - 1}}$$
$$SD = \sqrt{\sum \frac{(X_1 - \mu)^2}{n - 1}}$$

**3.2.3. Variance.**  
$$V = \sum \frac{(X - \mu)^2}{N}$$

Determinant of PCU (Tullu & Quezon, 2021) adopted dynamic method PCU for non-lane-based traffic movement of vehicles and heterogeneity of vehicular movement.

PCU = ((Vc/Vi)/(Ac/Ai))

Where:

Vc = mean speed of a car and Vi = mean speed of vehicle type i.

Ac = projected area of a vehicle and Ai = projected area of car vehicle i.

Table 5. Estimated Number of Traffic Flow Per Passenger Car Unit (P.C.U)

| Point 'A' Ma | raba-Abuja Ez | xpress Roa | d      |       | Point 'B' Ado-Abuja Expressway |           |        |       |
|--------------|---------------|------------|--------|-------|--------------------------------|-----------|--------|-------|
| Direction    | Total Both    | Direction  | P.C. U | Total | Total Both                     | Direction | P.C. U | Total |
| Vehicles     | NO            | %          | -      | -     | NO                             | %         | -      | -     |
| Trucks       | 255           | 0.60       | 4.38   | 384   | 79                             | 0.24      | 4.85   | 306   |
| Cars         | 5470          | 12.87      | 2.80   | 2747  | 2408                           | 7.36      | 3.00   | 3129  |
| Bus          | 442           | 1.04       | 3.25   | 332   | 278                            | 0.85      | 3.85   | 542   |
| Tricycle     | 2116          | 4.98       | 0.80   | 904   | 141                            | 0.43      | 0.75   | 155   |
| Motorcycle   | 23451         | 55.18      | 0.65   | 5887  | 24543                          | 75.01     | 0.95   | 15940 |
| Bicycle      | 72            | 0.17       | 0.43   | 11    | 95                             | 0.29      | 0.50   | 37    |
| Handcarts    | 1288          | 3.03       | 0.62   | 485   | 376                            | 1.15      | 0.75   | 365   |
| Pedestrian   | 9405          | 22.13      | 0.46   | 472   | 4800                           | 14.67     | 0.52   | 624   |
| Total        | 42499         | 100        | -      | 11222 | 32720                          | 100       | -      | 21098 |

Source: Author's, 2022

Table 6. Traffic flow along Maraba-Abuja Expressway (point 'A')

|        | 6:00-<br>700 | 7:00-<br>8:00 | 8:00-<br>9:00 | 9:00-<br>10:00 | 10:00-<br>11:00 | 11:00-<br>12:00 | 12:00-<br>1:00 | 1:00-<br>2:00 | 2:00-<br>3:00 | 3:00-<br>4:00 | 4:00-<br>5:00 | 5:00-<br>6:00 |       |
|--------|--------------|---------------|---------------|----------------|-----------------|-----------------|----------------|---------------|---------------|---------------|---------------|---------------|-------|
| Time   | am           | am            | am            | am             | am              | pm              | pm             | pm            | pm            | pm            | pm            | pm            | Total |
| T/Flow | 854          | 1708          | 3841          | 2561           | 1707            | 1067            | 854            | 854           | 1494          | 2134          | 3201          | 1067          | 21338 |
| %      | 4.0          | 8.0           | 18.0          | 12.0           | 8.0             | 5.0             | 4.0            | 4.0           | 7.0           | 10.0          | 15.0          | 5.0           | 100%  |

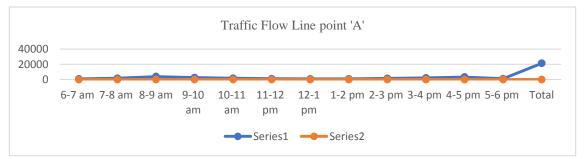
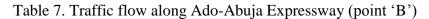


Figure 5. Traffic flow graph at point (A).

|        | 6:00-<br>7:00 | 7:00-<br>8:00 | 8:00-<br>9:00 | 9:00-<br>10:00 | 10:00-<br>11:00 | 11:00-<br>12:00 | 12:00-<br>1:00 | 1:00-<br>2:00 | 2:00-<br>3:00 | 3:00-<br>4:00 | 4:00-<br>5:00 | 5:00-<br>6:00 |       |
|--------|---------------|---------------|---------------|----------------|-----------------|-----------------|----------------|---------------|---------------|---------------|---------------|---------------|-------|
| Time   | am            | am            | am            | am             | am              | pm              | pm             | pm            | pm            | pm            | pm            | pm            | Total |
| T/Flow | 1402          | 1997          | 7777          | 4420           | 3442            | 2295            | 2507           | 2762          | 3570          | 7140          | 3655          | 1350          | 42499 |
| %      | 3.3           | 4.7           | 18.3          | 10.4           | 8.1             | 5.4             | 5.9            | 6.5           | 8.4           | 16.8          | 8.6           | 3.6           | 100%  |



|       |        |        |        |      | Traffi | c Flow | Line p | oint 'B <b>'</b> |          |           |           |       |
|-------|--------|--------|--------|------|--------|--------|--------|------------------|----------|-----------|-----------|-------|
| 60000 |        |        |        |      |        |        |        |                  |          |           |           |       |
| 40000 |        |        |        |      |        |        |        |                  |          |           |           | /     |
| 20000 |        |        |        |      |        |        |        |                  |          |           |           |       |
| 0     |        |        |        |      |        |        |        |                  |          |           |           |       |
|       | 6-7 am | 7-8 am | 8-9 am | 9-10 | 10-11  | 11-12  | 12-1   | 1-2 pm           | 2-3 pm 3 | -4 pm 4-5 | pm 5-6 pm | Total |
|       |        |        |        | am   | am     | pm     | pm     |                  |          |           |           |       |
|       |        |        |        |      | -      | T/Flo  | w –    | %                |          |           |           |       |
|       |        |        |        |      |        |        |        |                  |          |           |           |       |

Figure 6.Traffic flow graph at station (B).

# Hypothesis

 $H_o$ : There is statistical difference between traffic flow and travel time variability  $H_I$ : There is no statistical difference between traffic flow and travel time variability

| S/No | Traffic flow | Travel time (per hour) | Degree (s) | Variations |
|------|--------------|------------------------|------------|------------|
| 1    | 7083         | 1 hr, 30 minutes       | 3.15       | 0.66       |
| 2    | 5453         | 1hr, 45 minutes        | 2.82       | 0.60       |
| 5    | Speed        | 12.85                  | 9.57       | 3.31       |

Table 8. Result for the test of sample

Table 9. Travel time, speed, and travel distance Variability

| S/No  | Time (t)       | Speed (v) | Distance (km) | Variations |
|-------|----------------|-----------|---------------|------------|
| 1     | 1hr 15 minutes | 15 km/hr  | 54 km         | 3.60       |
| 2     | 1hr 45 minutes | 18 km/hr  | 54 km         | 3.00       |
| Total | 3:00 hrs       | 33 km/hr  | 108 km        | 6.60       |

| Table 10. Correlation coefficient of traffic flow and travel time | Table 10. Correlation | coefficient | of traffic f | flow and travel ti | me |
|---|-----------------------|-------------|--------------|--------------------|----|
|---|-----------------------|-------------|--------------|--------------------|----|

| S/No | Variables/      | $X^2$ | Degree of freedom | Variations |
|------|-----------------|-------|-------------------|------------|
| 1    | Time            | 3.83  | 3.15              | 0.66       |
| 2    | Traffic volume  | 3.42  | 2.82              | 0.60       |
| 3    | Traffic density | 2.94  | 2.23              | 0.71       |

| 4 | Traffic flow | 2.65  | 1.72 | 0.93 |  |
|---|--------------|-------|------|------|--|
| 5 | Speed        | 12.85 | 9.57 | 3.31 |  |

### **3.2.4.** Correlation coefficient.

$$r = \frac{n\sum xy - \sum x \sum y}{\sqrt{[n\sum x^2 - (\sum x)^2] [n\sum y^2 - (\sum y)^2]}}$$

Morning traffic flow point (A):  $f = \frac{21338}{12} = 1778$ Morning traffic flow pint (B):  $f = \frac{42499}{6}$  7083 Evening traffic flow  $f = \frac{32720}{6} = 5453$ Total flow = 42499 + 32720 = 75219 Average traffic flow =  $\frac{75219}{12} = 6268$ Travel time Speed:  $V = \frac{54}{75} = 0.75$ Time:  $T = \frac{54}{105} = 0.51$ Distance: S = s \* t = 12.85 \* 8.83 + 49.2 km



Figure 7. Congestion along Abuja-Kubwa



Figure 8 Congestion along Lagos Road



Figure 9. Congestion along Abuja-Nyanya



Figure 10. Congestion along Lagos Road

# 4.1. Discussion

Based on the findings of this study, it was discovered that when density was combined with other variables, longer travel times occurred on the Ado Highway between 8:00 a.m. and 9:00 a.m. in the morning and between 4:00 p.m. and 5:00 p.m. in the evening. The point, which is Maraba Highway, has a bite difference. During peak periods for the two locations, morning peaks occurred between 8:00 a.m. and 9:00 a.m., and evening peaks occurred between 3:00 p.m. and 5:00 p.m. These times denoted the point at which trip makers, or travellers who had recently left their origin (home), encountered serious travel time uncertainty.

In addition, apart from pedestrian movements, cars and motorcycles constitute the highest percentage of traffic (68.05%) at point A and 82.37% at point B. During the morning and evening peak periods, it takes between 25 and 40 minutes to get to point "A," while getting to point "B" takes between 15 and 25 minutes. The slow traffic point had an occasional traffic flow because of an oversized number of vehicles present at the time, whereas the fast-moving traffic point had the next highest traffic flow due to a better proportion of moving cars. The study revealed the following: the diversion of 15%-20% of the total traffic from the high-level congested roads to the results of the least or lesser congested roads into a higher level of service (lower congestion), an increase in speed by 15km/h to 20km/h from the current speed levels, and a decrease in travel time by 10%-15%, respectively. This study indicates that at point (A), the peak hourly period recorded between 8:00 - 9:00 am in the morning, and 4:00 pm - 5:00 pm during evening time. The second segment recoded 8:00 am at morning hours, and 3:00 pm - 4:00 pm at evening peak period.

### 5.0. Conclusions and Recommendations

Travel time variables are deemed to have high levels of consistency in order to assure drivers' smooth travel times; however, traffic flow, volume, speed, and density variation may lead to unanticipated delays. The variables of corridor highway travel time were identified in this study on Abacha Road, Karu, Nigeria, along the Abuja expressway. The study started by defining the problems associated with the variables of highway traffic reliability. The variables of travel time are also examined for different countries and their suitability.

Variables in corridor highway travel time pose global challenges to improving tripmaker reliability. In this proposal, travel time variables adopted in different countries were examined and compared to the study. In this research proposal, the current available corridor highway reliability variables include speed, travel time, traffic flow, traffic volume, traffic density, delay, level of services, weather, and traffic incidence. The study found that travel speed, traffic flow, density, volume, and travel time had a significant impact on corridor highway travel time reliability. The calculated variables were validated and compared to one another. The statistical mean was deemed significant at the 0.05% level (degree of freedom). Travel speed can also be computed using density and flow. The level of service was calculated by the minimum and maximum congestion. The results of all variables measured indicate no statistical relationships between the corresponding values.

### **References.**

- Abdulsattar, H., Mostafizi, A., Siam, M. R. K., & Wang, H. (2020). Measuring the impacts of connected vehicles on travel time reliability in a work zone environment: an agent-based approach. *Journal of Intelligent Transportation Systems: Technology, Planning, and Operations*, 24(5), 421–436. https://doi.org/10.1080/15472450.2019.1573351
- Afandizadeh Zargari, S., Amoei Khorshidi, N., Mirzahossein, H., & Kalantari, N. (2021). Comparative approach for predicting travel time reliability (a case study of Virginia interstate). *Innovative Infrastructure Solutions*, 6(4). https://doi.org/10.1007/s41062-021-00597-8
- Afrin, T., & Yodo, N. (2020). A survey of road traffic congestion measures towards a sustainable and resilient transportation system. *Sustainability (Switzerland)*, 12(11), 1–23. https://doi.org/10.3390/su12114660
- Arnott, R., & Small, K. (1994). The economics of traffic congestion. *American Scientist*, 82(5), 446–455. https://doi.org/10.4337/9781784712785
- Aven, T. (1988). Some considerations on reliability theory and its applications. *Reliability Engineering and System Safety*, 21(3), 215–223. https://doi.org/10.1016/0951-8320(88)90122-6
- Becker, G. (1965). A Theory of the ATime Allocation. In *The Economic Journal* (Vol. 75, Issue 299, pp. 493–517).
- Bimpou, K., & Ferguson, N. S. (2020). Dynamic accessibility: Incorporating day-to-day travel time reliability into accessibility measurement. *Journal of Transport Geography*, 89(January 2019), 102892. https://doi.org/10.1016/j.jtrangeo.2020.102892
- Chen, P., Tong, R., Lu, G., & Wang, Y. (2018). Exploring Travel Time Distribution and Variability Patterns Using Probe Vehicle Data: Case Study in Beijing. *Journal of Advanced Transportation*, 2018. https://doi.org/10.1155/2018/3747632
- Chen, Z., & Fan, W. (2021). A freeway travel time prediction method based on an xgboost model. *Sustainability (Switzerland)*, *13*(15). https://doi.org/10.3390/su13158577
- Chen, Z., Liu, X. C., Farnsworth, G., & Burns, K. (2019). Validating the Adaptability of Travel Time Reliability MeaChen, Z., Liu, X. C., Farnsworth, G., & Burns, K. (2019). Validating the Adaptability of Travel Time Reliability Measurements using Probe Data. Transportation Research Record, 2673(6), 57–67. https. *Transportation Research Record*, 2673(6), 57–67. https://doi.org/10.1177/0361198119843097

- Chidera, G. (2020). Vehicular Traffic Congestion in Selected Satellite Towns in the Federal Capital Territory (FCT) Abuja, Nigeria ALPHONSUS NWACHUKWU ALI. 25(7), 49–60. https://doi.org/10.9790/0837-2507014960
- Chung, W., Abdel-Aty, M., Park, H. C., Cai, Q., Rahman, M., Gong, Y., & Ponnaluri, R. (2020). Development of Decision Support System for Integrated Active Traffic Management Systems Considering Travel Time Reliability. *Transportation Research Record*, 2674(2), 167–180. https://doi.org/10.1177/0361198120905591
- D'Este, G. M., Zito, R., & Taylor, M. A. P. (1999). Using GPS to measure traffic system performance. *Computer-Aided Civil and Infrastructure Engineering*, 14(4), 255–265. https://doi.org/10.1111/0885-9507.00146
- Federal Highway Administration. (1991). Chapter 1- Federal Highway Association. *Travel Time Data Collection Handbook*, 1–10. https://www.fhwa.dot.gov/ohim/handbook/chap1.pdf
- FHWA. (2019). *Does Travel Time Reliability Matter? October*, 64p. https://ops.fhwa.dot.gov/publications/fhwahop19062/fhwahop19062.pdf%0Ahttps://rosap.ntl. bts.gov/view/dot/43597%0Ahttps://trid.trb.org/view/1674280
- Fulari, S., Thankappan, A., Vanajakshi, L., & Subramanian, S. (2019). Traffic flow estimation at error prone locations using dynamic traffic flow modeling. *Transportation Letters*, 11(1), 43– 53. https://doi.org/10.1080/19427867.2016.1271761
- Gaver, D. P. (1968). Headstart Strategies for Combating Congestion. *Transportation Science*, 2(2), 172–181. https://doi.org/10.1287/trsc.2.2.172
- Hameed, S., Khan, F. I., & Hameed, B. (2019). Understanding Security Requirements and Challenges in Internet of Things (IoT): A Review. In *Journal of Computer Networks and Communications* (Vol. 2019). Hindawi Limited. https://doi.org/10.1155/2019/9629381
- Ibarra-Espinosa, S., Ynoue, R., Giannotti, M., Ropkins, K., & de Freitas, E. D. (2019). Generating traffic flow and speed regional model data using internet GPS vehicle records. *MethodsX*, 6, 2065–2075. https://doi.org/10.1016/j.mex.2019.08.018
- Incorporating Reliability Performance Measures into the Transportation Planning and Programming Processes. (2013). In *Incorporating Reliability Performance Measures into the Transportation Planning and Programming Processes*. https://doi.org/10.17226/22596
- Indian Roads Congress. (1990). Guidelines for Capacity of Urban Roads in Plain Areas. New Delhi. In *IRC Code of Practice* (Vol. 106).
- Jabari, S. E. G., Dilip, D. M., Lin, D., & Thonnam Thodi, B. (2019). Learning Traffic Flow Dynamics Using Random Fields. *IEEE Access*, 7, 130566–130577. https://doi.org/10.1109/ACCESS.2019.2941088
- Kathuria, A., Parida, M., & Sekhar, C. R. (2017). Route performance evaluation of a closed bus rapid transit system using GPS data. *Current Science*, *112*(8), 1642–1652. https://doi.org/10.18520/cs/v112/i08/1642-1652
- Kathuria, A., Parida, M., & Sekhar, C. R. (2020). A Review of Service Reliability Measures for Public Transportation Systems. *International Journal of Intelligent Transportation Systems Research*, 18(2), 243–255. https://doi.org/10.1007/s13177-019-00195-0
- Khoo, W. C., Lim, K. S., & Cheong, H. T. (2021). Travel Time Reliability Modelling with Burr Distribution. *Malaysian Journal of Mathematical Sciences*, *15*(2), 313–322.
- Kidando, E., Moses, R., Sando, T., & Ozguven, E. E. (2019). Assessment of factors associated with travel time reliability and prediction: an empirical analysis using probabilistic reasoning approach. *Transportation Planning and Technology*, 42(4), 309–323. https://doi.org/10.1080/03081060.2019.1600239
- Knight, T. (1974). AN A P P R O A C H TO THE E V A L U A T I O N OF CHANGES IN T R A V

*E L measured generalised costs by different modes of travel are identical but the probabilities of choosing either mode are different*. *Differences in the reliability of the various modes*. *3*, 393–407.

- Kong, X., Eisele, W. L., Zhang, Y., & Cline, D. B. H. (2018). Evaluating the Impact of Real-Time Mobility and Travel Time Reliability Information on Truck Drivers' Routing Decisions. *Transportation Research Record*, 2672(9), 164–172. https://doi.org/10.1177/0361198118797508
- Li, H., He, F., Lin, X., Wang, Y., & Li, M. (2019). Travel time reliability measure based on predictability using the Lempel–Ziv algorithm. *Transportation Research Part C: Emerging Technologies*, 101(February), 161–180. https://doi.org/10.1016/j.trc.2019.02.014
- Li, S., Liu, C., & Chang, F. (2022). Time-Spatial Multiscale Net for Vehicle Counting and Traffic Volume Estimation. *IEEE Transactions on Cognitive and Developmental Systems*, 14(2), 740–751. https://doi.org/10.1109/TCDS.2021.3073694
- Lomax, T., Schrank, D., Turner, S., & Margiotta, R. (2003). Selecting travel reliability measures. *Texas Transportation Institute*, *May 2003*, 43. https://static.tti.tamu.edu/tti.tamu.edu/documents/TTI-2003-3.pdf
- Lu, L., Wang, J., Wu, Y., Chen, X., & Chan, C. Y. (2021). A Real-Time Prediction Model For Individual Vehicle Travel Time on an undersaturated Signalized Arterial Roadway. *IEEE Intelligent Transportation Systems Magazine*, *April 2021*, 72–87. https://doi.org/10.1109/MITS.2021.3068416
- Macioszek, E. (2019). The passenger car equivalent factors for heavy vehicles on turbo roundabouts. *Frontiers in Built Environment*, 5(May). https://doi.org/10.3389/fbuil.2019.00068
- Maghrour Zefreh, M., & Török, Á. (2020). Distribution of traffic speed in different traffic conditions: An empirical study in budapest. *Transport*, 35(1), 68–86. https://doi.org/10.3846/transport.2019.11725
- Nicholson, A. (2003). Transport Network Reliability Measurement and Analysis. In *Transportes* (Vol. 11, Issue 2). https://doi.org/10.14295/transportes.v11i2.148
- Nnamani, O. J., Ijaware, V. A., Olusina, J. O., & Idowu, T. O. (2020). Model for Estimating Travel Time on Dynamic Highway Networks in Akure, Ondo State Nigeria. *European Journal of Engineering Research and Science*, *5*(3), 275–281. https://doi.org/10.24018/ejers.2020.5.3.1671
- No, R., & For, P. (2022). FORECASTING TRAVEL-TIME RELIABILITY Prepared For: Utah Department of Transportation. February.
- Olszewski, P., Dybicz, T., Jamroz, K., Kustra, W., & Romanowska, A. (2018). Assessing highway travel time reliability using probe vehicle data. *Transportation Research Record*, 2672(15), 118–130. https://doi.org/10.1177/0361198118796716
- Otuoze, S. H., Hunt, D. V. L., & Jefferson, I. (2021). Predictive modeling of transport infrastructure space for urban growth phenomena in developing countries' cities: A case study of Kano-Nigeria. *Sustainability (Switzerland), 13*(1), 1–20. https://doi.org/10.3390/su13010308
- Rivera-Royero, D., Galindo, G., Jaller, M., & Betancourt Reyes, J. (2022). Road network performance: A review on relevant concepts. *Computers and Industrial Engineering*, 165(January). https://doi.org/10.1016/j.cie.2021.107927
- Roess, R. P., Vandehey, M. A., & Kittelson, W. (2010). Level of service: 2010 and beyond. *Transportation Research Record*, 2173, 20–27. https://doi.org/10.3141/2173-03
- Romanowska, A., & Jamroz, K. (2021). Comparison of traffic flow models with real traffic data

based on a quantitative assessment. *Applied Sciences (Switzerland)*, 11(21). https://doi.org/10.3390/app11219914

- Samal, S. R., Gireesh Kumar, P., Cyril Santhosh, J., & Santhakumar, M. (2020). Analysis of Traffic Congestion Impacts of Urban Road Network under Indian Condition. *IOP Conference Series: Materials Science and Engineering*, 1006(1). https://doi.org/10.1088/1757-899X/1006/1/012002
- Shelke, H., Lokhande, V., Pawar, A., Solanke, M., & Ghodke, T. (2022). EPRA International Journal of Research and Development (IJRD) TRAFFIC CONGESTION PREDICTION THROUGH DEEP LEARNING. 7838(January), 34–37. https://doi.org/10.36713/epra2016
- Siddiqui, C., & Ko, K. (2020). Exploratory Analysis of the Relationships between Congestion, Travel Time Reliability, and Freight-Related Performance Management Measures and Their Associativity with the Roadway Attributes. *Transportation Research Record*, 2674(10), 571– 582. https://doi.org/10.1177/0361198120937692
- Steinmaßl, M., Kranzinger, S., & Rehrl, K. (2021). Analyzing travel time reliability from sparse probe vehicle data: A case study on the effects of spatial and temporal aggregation. *Transportation Research Record*, 2675(12), 832–849. https://doi.org/10.1177/03611981211031538
- Susilawati, S., Student, P., Taylor, M. A. P., & Somenahalli, S. V. C. (2010). Travel Time Reliability Measurement for Selected Corridors in the Adelaide Metropolitan Area. *Journal of the Eastern Asia Society for Transportation Studies*, 8, 86–102.
- Taylor, M. A. P., & Susilawati. (2012). Modelling Travel Time Reliability with the Burr Distribution. *Procedia Social and Behavioral Sciences*, 54, 75–83. https://doi.org/10.1016/j.sbspro.2012.09.727
- Texas Transportation Institute, & Cambridge Systems, I. (2006). Travel time reliability. In *Federal Highway Administration, U.S. Department of Transportation*.
- Transportation Research Board. (2010). Highway Capacity Manual.
- Tsuboi, T. (2021). Visualization and analysis of traffic flow and congestion in India. *Infrastructures*, 6(3), 1–13. https://doi.org/10.3390/infrastructures6030038
- Tufuor, E. O. A., & Rilett, L. R. (2019). Validation of the Highway Capacity Manual Urban Street Travel Time Reliability Methodology using Empirical Data. *Transportation Research Record*, 2673(4), 415–426. https://doi.org/10.1177/0361198119838854
- Tufuor, E. O. A., & Rilett, L. R. (2020). Analysis of Component Errors in the Highway Capacity Manual Travel Time Reliability Estimations for Urban Streets. *Transportation Research Record*, 2674(6), 85–97. https://doi.org/10.1177/0361198120917977
- Tufuor, E. O. A., & Rilett, L. R. (2021). New travel time reliability methodology for urban arterial corridors. *Transportation Research Record*, 2675(9), 1106–1117. https://doi.org/10.1177/03611981211006104
- Tufuor, E., Rilett, L., & Murphy, S. (2021). Validating and calibrating the highway capacity manual arterial travel time reliability methodology. *Transportation Research Record*, 2675(11), 1382–1399. https://doi.org/10.1177/03611981211026663
- Tullu, H. H., & Quezon, E. T. (2021). Determination of Passenger Car Unit for Urban Roads: A Case Study in Addis Ababa. SSRN Electronic Journal, 5(2), 57–63. https://doi.org/10.2139/ssrn.3931154
- Wang, W., & Guo, R. (2022). Travel Time Reliability of Highway Network under Multiple Failure Modes. Sustainability, 14(12), 7256. https://doi.org/10.3390/su14127256
- Wu, Z., Rilett, L. R., & Ren, W. (2022). New methodologies for predicting corridor travel time mean and reliability. *International Journal of Urban Sciences*, 26(3), 517–540. https://doi.org/10.1080/12265934.2021.1899844
- Zhang, X., Lauber, L., Liu, H., Shi, J., Xie, M., & Pan, Y. (2022). Travel time prediction of urban

public transportation based on detection of single routes. *PLoS ONE*, *17*(1 January 2022), 1–23. https://doi.org/10.1371/journal.pone.0262535

Zheng, F., Li, J., van Zuylen, H., Liu, X., & Yang, H. (2018). Urban travel time reliability at different traffic conditions. *Journal of Intelligent Transportation Systems: Technology, Planning, and Operations, 22*(2), 106–120. https://doi.org/10.1080/15472450.2017.1412829

Zimmer, W. J., Keats, J. B., & Wang, F. K. (1998). The burr XII distribution in reliability analysis. *Journal of Quality Technology*, *30*(4), 386–394. https://doi.org/10.1080/00224065.1998.11979874