



Seismic Performance Evaluation of Indian code-designed Concrete Moment Resisting Frames using PBSE Procedures

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Performance-based seismic design framework has provided various procedures to assess the performance of structures exposed to seismic loads. Based on the structural and non-structural components' degree of damage, these approaches have recognized different building performance levels. The analytical compatibility of these approaches depends upon a number of parameters includes modeling of structural members, location of plastic hinges, applied lateral load patterns, effects of damping and vibration's natural period. The performance-based seismic evaluation processes described in the performance-based seismic design framework are thoroughly examined in this paper. These methods are compared for group of seventy-five reinforced concrete frames representing low, medium and high-rise structures design as per the guidelines of Indian seismic codes. Performances of these example moment-resisting frames are compared and parametric studies of engineering demand parameters are carried out. The possible gray areas for integration of performance evaluation and assessment have been put forth.

Keywords: Performance-based seismic evaluation procedures, example MRFs, pushover analysis, parametric studies

Introduction

Seismic design is a two-step process; firstly, the preliminary structural configuration is selected; followed by the evaluation of the capacity of the adopted structural configuration. If the capacity of the selected structural system meets the needed demand, then the designs are finalized. Otherwise revision in the design is done. The procedure is repeated till desired performance is reached [FEMA 445,2005; Ghobarah A., 2001 and Zameeruddin and Sangle, 2016]. Reinforced Concrete Moment Resisting Frames (RCMRFs) are commonly used for lateral load carrying systems in seismically active zones. In India, IS 1893 and IS 13920 are usually used in all states

to govern seismic design and construction of RCMRFs. These codes are aimed at setting forth the basic requirements for safety of life (ductility and strength) and control of damage (serviceability drift limits) against seismic hazards. [Erduran and Yakut, 2007; Zameeruddin and Sangle, 2017a]. [Mondal, A., Ghosh, S., Reddy, G.R.,2013].

By using force-based (FBD) design requirements, which necessitate that forces and displacements remain within elastic limits, the intended outcome is achieved. When exposed to earthquakes, these structures exhibit inelastic behavior, that has been addressed by incorporating a response reduction factor to forces and displacements. Nevertheless, this indirect practice results in an incorrect assessment of the actual building response. Structures designed following these code provisions were found to get damaged or collapse during strong and moderate seismic events, thereby questioning the safety of structure and humans [Zameeruddin and Sangle, 2016; Murty et al., 2012].

Structure's seismic response is governed by the structural components' performance to withstand earthquakes. The key components of a structural system are those which form lateral load path and vertical stability. When subjected to seismic hazards they experience inelastic incursions, which may lead towards failure of individual components or redistribution among groups of members leading to collapse of the complete structure. More than a half century, assessment of structural performance is becoming more significant in order to reflect how structures perform when subjected to seismic hazard. Primary goal of this methodology is to identify various structural performance levels. FEMA 445 has described sequential steps involved in PBSA as shown in figure 1 [FEMA 445,2006].

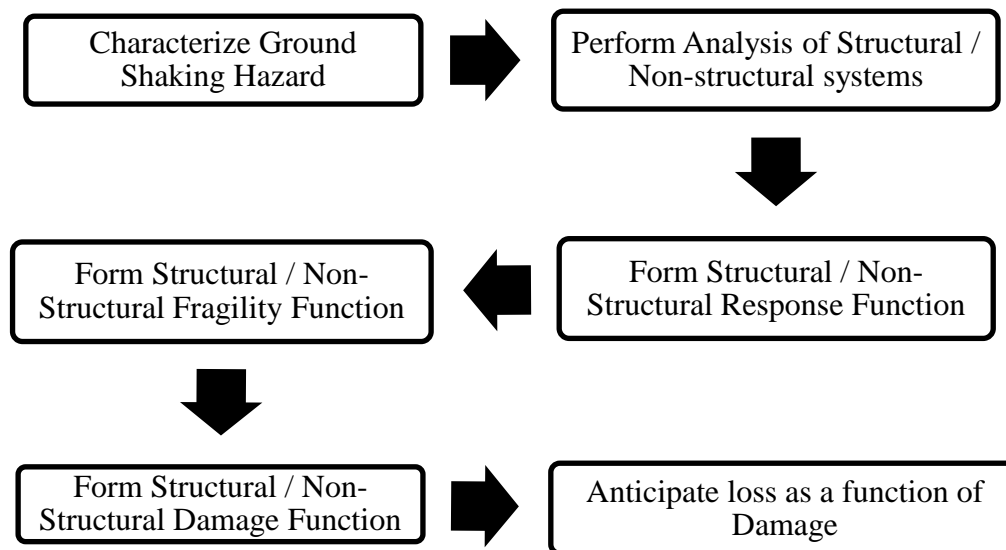


Fig.1: Performance Evaluation Process

Performance-based Seismic Assessment (PBSA) procedures use damage indices to assess the damages sustained by structure at local and global levels. These damage indices are evaluated by

two approaches; (a) probabilistic and (b) deterministic. In a probabilistic method the dynamic characteristics of structures are considered. In a deterministic method various engineering demand parameter are considered to assess the state of damage. These engineering parameters include strength, stiffness, dissipated energy, curvature, deformation, base shear, stress, strain, and displacement. The damage index scales the damage value from "0" to "1," depending upon the degree of damages occurred to the structures. Where the "0" denotes no damage state and "1" denotes a collapsed state [Zameeruddin and Sangle, 2021a; Azhdary and Shabakty, 2014; Borg and Rossetto, 2010].

Performance-based Seismic Evaluation (PBSE) methodologies described in the PBSD framework assess the performance of structure based on collapse mechanism. The plastic hinges envelopes and their transition from one level of performance to the next level are represented by this collapse mechanism. The performance levels do not scale up the damage value even if they are stated as a result of damages to both structural and non-structural components. There exists an identified gray area for linking damage values with collapse mechanisms.

Performance-based Seismic Evaluation Procedures

Soft computing techniques have advanced in civil engineering, enabling researchers to undertake more complex seismic analyses with increased analysis accuracy. Two widely used PBSE approaches, the "Capacity Spectrum Method (CSM)" and the "Displacement Coefficient Method (DCM)," are presented in PBSD documentation [Boroujeni, A.R.K., 2013]. When using CSM, inelastic displacements are evaluated by comparing a structure's capacity with the demands placed on it by an earthquake's ground motion. By performing a Pushover Analysis (POA) on inelastic SDOF systems, it is possible to acquire the displacement spectra and an inelastic strength required to determine an earthquake demand. This method acknowledges that the structure's effective period and its effective damping will increase as the structure is shaken exceeding its yield point.

It is predicted that the point at which capacity curve and demand spectrum intersect one another, exhibit the highest structural response. Performance Point is the name designated to the intersection. With this approach, the 5% damped elastic ground motion spectrum is intended to be reduced to a lower spectrum that corresponds to the structure's response. For a particular ground motion, the structural response can be evaluated by finding the higher acceleration and displacement on the capacity curve that agrees with the ground motion requirement at the higher level of damping and longer period which the structure experiences. The approach is updated in FEMA 440. With the intention of publishing a more precise seismic evaluation, the new FEMA is presented. Figure 2 describes CSM procedure recommended in ATC 40 and FEMA 440 [Korkmaz and Irtem, 2008; Boroujeni, 2013].

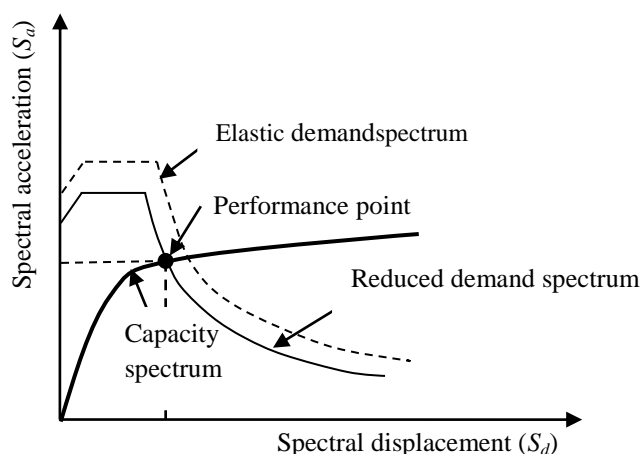


Fig. 2(a): Assessment of performance point as per ATC 40

DCM utilizes ductility to determine the highest value of displacement. The approach offers an arithmetic procedure for estimating out the displacement demand. The capacity curve does not need to be converted into spectral coordinates. The nonlinear force-displacement relationship that exists between base shear and displacement must be substituted by an idealized relationship in order to calculate the structure's effective yield strength V_y and effective lateral stiffness K_e . The bilinear aspect of this relationship is defined by an initial slope of K_e and a post-yield slope of K_s . It is necessary to select line segments on the idealized force-displacement curve using an iterative graphical method that approximately balances the area below and above the curve. Structure's effective lateral stiffness, K_e , is considered as the secant stiffness determined at the base shear force that is equivalent to 60% of the effective yield strength V_y , of the structure. Idealized force-displacement curve is considered as a basis for the effective fundamental period in the direction under consideration. [Chopra and Goel, 2000; ASCE/SEI 41, 2007]. Figure 3 illustrated the DCM procedures described in FEMA 273 and ASCE 41.

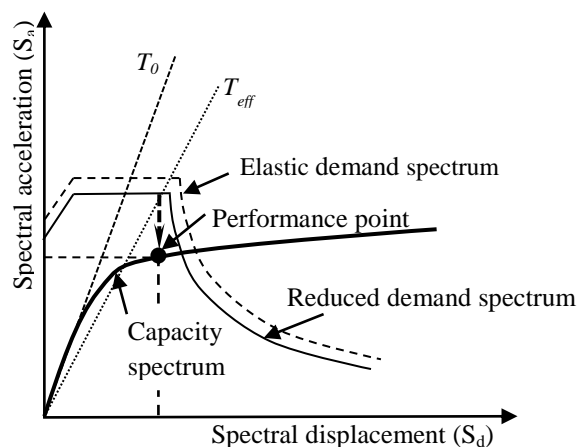


Fig 2 (b): Assessment of performance point by improved CSM

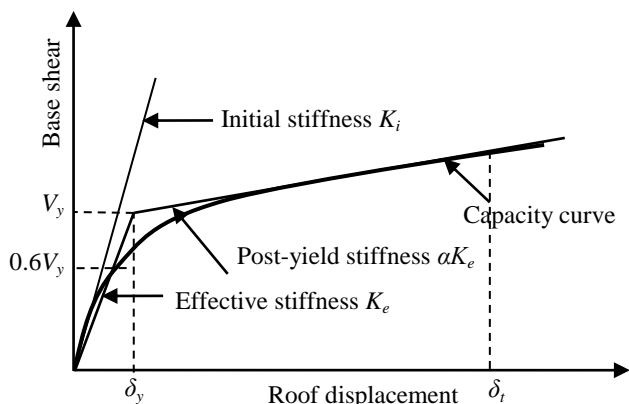


Fig. 3 (a): Calculation of target displacement as FEMA 273

All of the PBSE processes described in PBSO can give the structure's collapse mechanism, but they cannot produce any damage value on their own. In this research, an attempt has been made to acquire damage values for example MRFs subjected to lateral loads analyze for PBSE procedures. Damages are quantified using engineering demand parameters resulting in PBSE output [Zameeruddin and Sangle, 2021b]

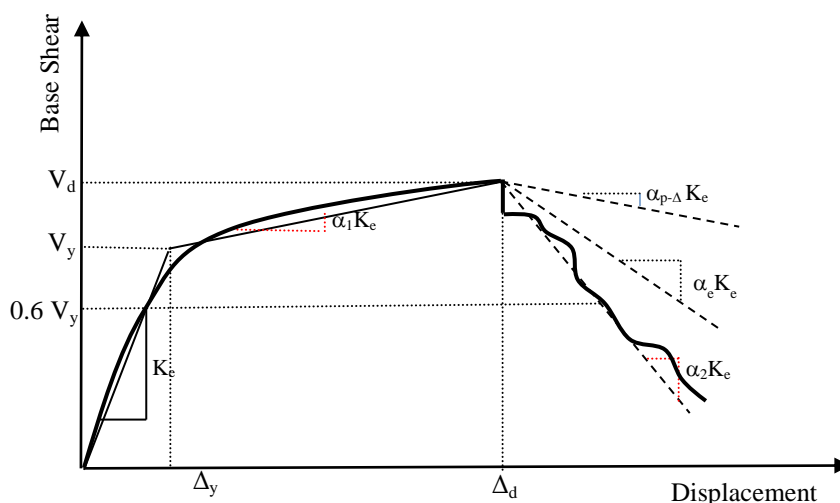


Fig. 3 (b): Idealized force-displacement curves in ASCE-41

Example RCMRFs

In this study, seventy-five example RCMRFs that represent the overall construction trend used in India have had their performance evaluated. PBSE techniques outlined in PBSO were used to assess the performance of these RCMRFs. The example RCMRFs are grouped into different categories on the basis of increasing numbers of storeys and bays. The typical bay width and storey height are both 3 m. It is believed that there are 3m between each frame. According to IS 1893, these RCMRFs depict a typical office building situated in the seismic zone "V" on a medium soil type. These RCMRFs are a representation of low, medium, and high-rise structures.

These example RCMRFs structures were analytically modelled using SAP 2000V 17.0. (Wilson and Habibullah, 2000).

The example RCMRFs structural components material characteristics are shown in Table 1 and the typical layout of the example RCMRFs is shown in Fig. 4. The design of these RCMRFs complies with the ductile detailing requirements specified in IS 456 and IS 1786 and IS 13920. Design details for structural components are given in Table 2. In Table 3, these MRFs' characteristics are listed.

The calculated demand is not the only one that can be addressed by the structural design of these RCMRFs. Several designers could propose possible approaches based on the same demand. The structural component designs used in this work were based on typical methods used by Indian engineers. For a planar frame, up to the first three storeys, all columns and beams in the story have the same section or have opted to stay the same, and then incremental changes in cross-sections are made. Design considerations taken into account the strong-column-weak-behaviors criterion.

These RCMRFs were put through a number of lateral load patterns, such as (a) the trivial lateral load pattern prescribed by IS 1893 consider as load case Push 1, (b) the uniform lateral load pattern considers as load case Push 2 and (c) the elastic first mode lateral load pattern considers as load case Push 3. Different lateral load patterns adopted in POA are displayed in Figure 5.

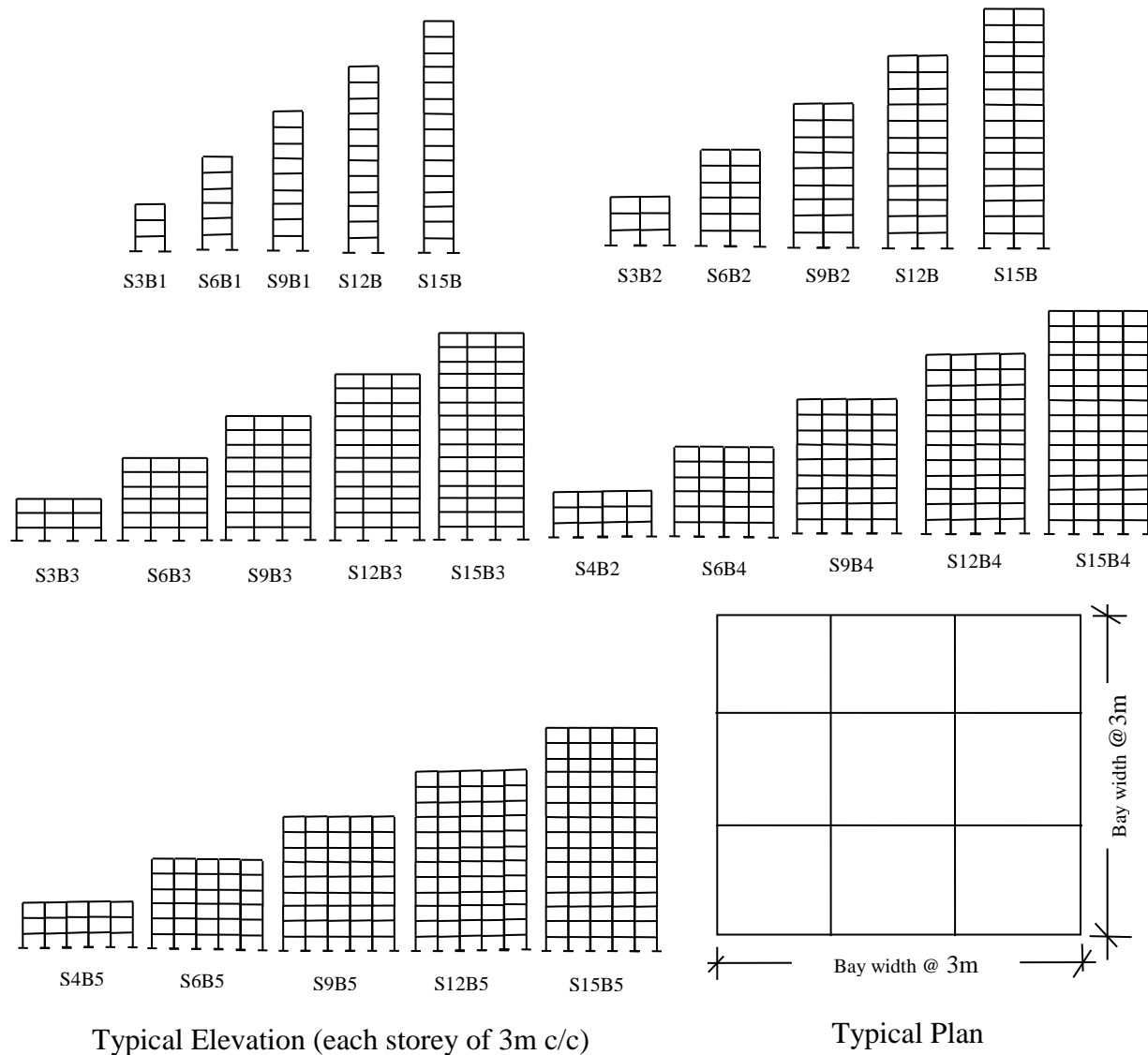


Table 1: Material properties of MRFs consider for design [IS 456 and IS 1786]

| Material property of MRFs | Concrete Grade, M 25 | Steel Grade, Fe 415 |
|---|----------------------|---------------------|
| Weight per unit volume (KN/m ³) | 25 | 76.97 |
| Mass per unit volume (Kg/m ³) | 2.548 | 7.849 |
| Modulus of elasticity (KN/m ²) | 25E+ 06 | 2E + 08 |
| Characteristic strength (KN/m ²) | 25000 | 45000 (yield) |
| Minimum tensile strength (KN/m ²) | - | 485,800 |
| Expected yield strength (KN/m ²) | - | 465,500 |
| Expected tensile strength(KN/m ²) | - | 533,500 |

The design base shears of RCMRFs were obtained by following the guidelines of IS 1893. The following formula is utilized for estimating a building's design base shear:

$$V_d = \frac{ZIS_a}{2Rg} W_i$$

Where; Z is 0.36 (zone factor), I is the structure's importance factor taken as 1 for these RCMRFs, R is taken as 5, W is the structure's seismic weight, and S_a is the spectral acceleration with respect to 5% damping.

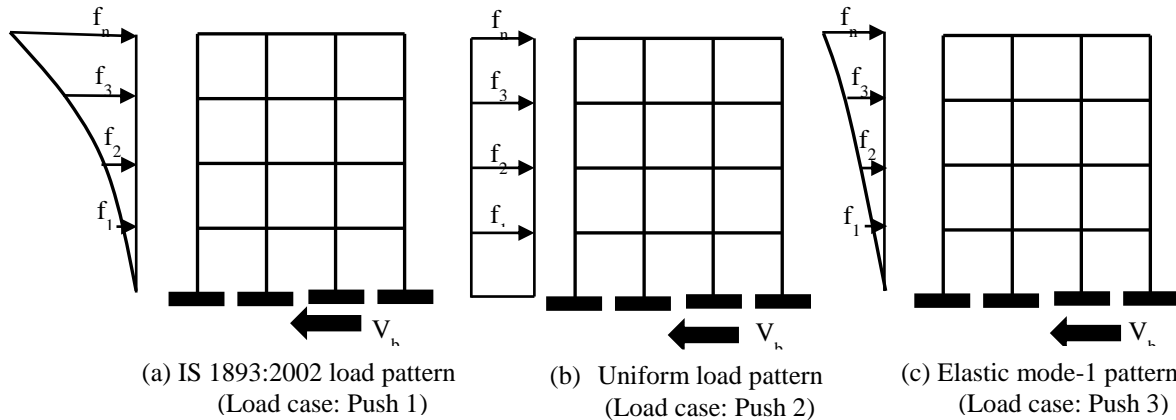


Fig. 5. Different load patterns for pushover

Table 2: Details of the Reinforced Concrete section for the example RCMRFs

| Group | RCMRFs | Stories | Column | | Beam | |
|-------|--------|---------|------------|------------|------------|------------|
| | | | Width (mm) | Depth (mm) | Width (mm) | Depth (mm) |
| I | S3B1 | 1 - 3 | 680 | 680 | 300 | 450 |
| | S6B1 | 3 - 6 | 600 | 600 | 300 | 450 |
| | S9B1 | 7 - 9 | 530 | 530 | 300 | 380 |
| | S12B1 | 10 - 12 | 450 | 450 | 300 | 380 |
| | S15B1 | 13 - 15 | 300 | 300 | 300 | 300 |
| II | S3B2 | 1 - 3 | 680 | 680 | 300 | 450 |
| | S6B2 | 3 - 6 | 600 | 600 | 300 | 450 |
| | S9B2 | 7 - 9 | 530 | 530 | 300 | 380 |
| | S12B2 | 10 - 12 | 450 | 450 | 300 | 380 |
| | S15B2 | 13 - 15 | 300 | 300 | 300 | 300 |
| III | S3B3 | 1 - 3 | 680 | 680 | 300 | 450 |
| | S6B3 | 3 - 6 | 600 | 600 | 300 | 450 |
| | S9B3 | 7 - 9 | 530 | 530 | 300 | 380 |

| | | | | | | |
|-------|---------|---------|-----|-----|-----|-----|
| IV | S12B3 | 10 - 12 | 450 | 450 | 300 | 380 |
| | S15B3 | 13 - 15 | 300 | 300 | 300 | 300 |
| | S3B4 | 1 - 3 | 680 | 680 | 300 | 450 |
| | S6B4 | 3 - 6 | 600 | 600 | 300 | 450 |
| | S9B4 | 7 - 9 | 530 | 530 | 300 | 380 |
| | S12B4 | 10 - 12 | 450 | 450 | 300 | 380 |
| V | S15B4 | 13 - 15 | 300 | 300 | 300 | 300 |
| | S3B5 | 1 - 3 | 680 | 680 | 300 | 450 |
| | S6B5 | 3 - 6 | 600 | 600 | 300 | 450 |
| | S9B5 | 7 - 9 | 530 | 530 | 300 | 380 |
| | S12B5 | 10 - 12 | 450 | 450 | 300 | 380 |
| S15B5 | 13 - 15 | 300 | 300 | 300 | 300 | |

The terms S and B specify the number of stories and bays, respectively.

Table 3: Characteristics of the studied example RCMRFs

| Group | MRF | h_i (m) | T_m (S) | T_d (S) | S_a/g | W_i (kN) | V_b (kN) |
|-------|-------------|-----------|--------------|--------------|-------------|----------------|---------------|
| I | S3B1 | 9 | 0.213 | 0.390 | 2.50 | 379.28 | 34.13 |
| | S6B1 | 18 | 0.508 | 0.655 | 2.49 | 753.90 | 67.85 |
| | S9B1 | 27 | 0.840 | 0.888 | 1.83 | 1088.04 | 63.40 |
| | S12B1 | 36 | 1.225 | 1.102 | 1.48 | 1387.03 | 55.44 |
| | S15B1 | 45 | 1.637 | 1.303 | 1.25 | 1630.02 | 48.75 |
| II | S3B2 | 9 | 0.216 | 0.390 | 2.50 | 671.76 | 60.45 |
| | S6B2 | 18 | 0.493 | 0.655 | 2.49 | 1339.92 | 120.59 |
| | S9B2 | 27 | 0.792 | 0.888 | 1.83 | 1945.25 | 120.23 |
| | S12B2 | 36 | 1.130 | 1.102 | 1.48 | 2497.68 | 108.22 |
| | S15B2 | 45 | 1.495 | 1.303 | 1.25 | 2963.40 | 97.07 |
| III | S3B3 | 9 | 0.217 | 0.390 | 2.50 | 964.30 | 86.78 |
| | S6B3 | 18 | 0.488 | 0.655 | 2.49 | 1926.05 | 173.34 |
| | S8B3 | 24 | 0.674 | 0.813 | 2.03 | 2510.32 | 182.42 |
| | S9B3 | 27 | 0.776 | 0.888 | 1.83 | 2802.46 | 176.85 |
| | S12B3 | 36 | 1.097 | 1.102 | 1.48 | 3608.33 | 161.09 |
| | S15B3 | 45 | 1.443 | 1.303 | 1.25 | 4296.79 | 145.75 |
| IV | S3B4 | 9 | 0.217 | 0.390 | 2.50 | 1256.84 | 113.11 |

| | | | | | | | |
|---|-------|----|-------|-------|------|---------|--------|
| | S6B4 | 18 | 0.485 | 0.655 | 2.49 | 2512.18 | 226.09 |
| | S9B4 | 27 | 0.768 | 0.888 | 1.83 | 3659.67 | 233.34 |
| | S12B4 | 36 | 1.080 | 1.102 | 1.48 | 4718.98 | 213.84 |
| | S15B4 | 45 | 1.418 | 1.303 | 1.25 | 5630.18 | 194.33 |
| V | S3B5 | 9 | 0.217 | 0.390 | 2.50 | 1549.38 | 139.44 |
| | S6B5 | 18 | 0.484 | 0.655 | 2.49 | 3098.31 | 278.84 |
| | S9B5 | 27 | 0.763 | 0.888 | 1.83 | 4516.88 | 289.77 |
| | S12B5 | 36 | 1.071 | 1.102 | 1.48 | 5829.64 | 266.50 |
| | S15B5 | 45 | 1.404 | 1.303 | 1.25 | 6963.57 | 242.83 |

Pushover Analysis

POA is performed in two steps: (i) RCMRFs are subjected to gravity loads with a load case of dead loads plus 50percent live loads (force-control), and (ii) the structure's state from the first step is recalled and subjected to a pattern of lateral loads applied to a structure with a controlled displacement of 4% corresponding to the structure's height (displacement-control). A dead load of intensity 18 kN/m and a live load of intensity 4.5 kN/m were applied to all floors. The results of the S8B3 RCMRF are discussed in detail among the seventy-five example RCMRFs. The lateral forces of S8B3 RCMRFs are summarized in Table 4.

Table 4: Lateral loads acting on the example S8B3 RCMRF

| Story level | Story height (m) | Story weight (kN) | $W_i h_i^2$ | $Q_i = V_b \frac{W_i h_i^2}{\sum W_i h_i^2}$ (kN) | Obtained from SAP 2000 |
|-----------------------|------------------|-------------------|-------------|---|------------------------|
| Roof | 24 | 2510.32 | 263775261.9 | 75.501 | 46.205 |
| 7 th floor | 21 | 2218.18 | 183787000.3 | 52.606 | 44.979 |
| 6 th floor | 18 | 1926.04 | 108173512.1 | 30.963 | 34.922 |
| 5 th floor | 15 | 1605.46 | 52194758.46 | 14.94 | 25.183 |
| 4 th floor | 12 | 1284.88 | 21395842.32 | 6.124 | 16.117 |
| 3 rd floor | 9 | 964.29 | 6778756.91 | 1.940 | 9.500 |
| 2 nd floor | 6 | 613.01 | 1217493.54 | 0.348 | 4.415 |
| 1 st floor | 3 | 281.95 | 2537.604 | 0.0007 | 1.104 |

The equivalent static method (IS 1893) and SAP yield nearly equal base shear. According to IS 1893, the lateral load distribution is a trivial load pattern, with lateral load expanding with storey height. The SAP results demonstrate the normalization of lateral loads along the building's height. These discrepancies may be accounted for by the incorporation of higher mode effects. This is the reason why we used 3 distinct load patterns to obtain both lower and upper bound values for example RCMRFs.

The moment-curvature (M- θ) behavior of the RCMRFs' members plays a major role in determining their nonlinear behavior. The moment-rotation (M- θ) relationship in SAP 2000 is necessary for nonlinear modelling in place of the moment-curvature relationship. The software's built-in stress-strain relationship, FEMA 356, was used to generate the default hinge's M- θ curve.

The contra-flexure point is often found in the middle of the members in an RCMRF with lateral loads. In a lumped plasticity model, several researchers think that plastic hinge generation at both ends of the member is best suited for POA. In the current study, concentrated M3 and P-M3 plastic hinges are integrated at both ends of the beams and columns. Figure 6 shows the acceptance standards for maximum rotational capacity, symbolized by the letters IO, LS, and CP. The modelling parameters and numerical acceptability standards are provided in Tables 5 and 6. These factors are affected by sectional characteristics like area of cross-section, percentage of rebar in compression and tension, design axial loads and design shear strength.

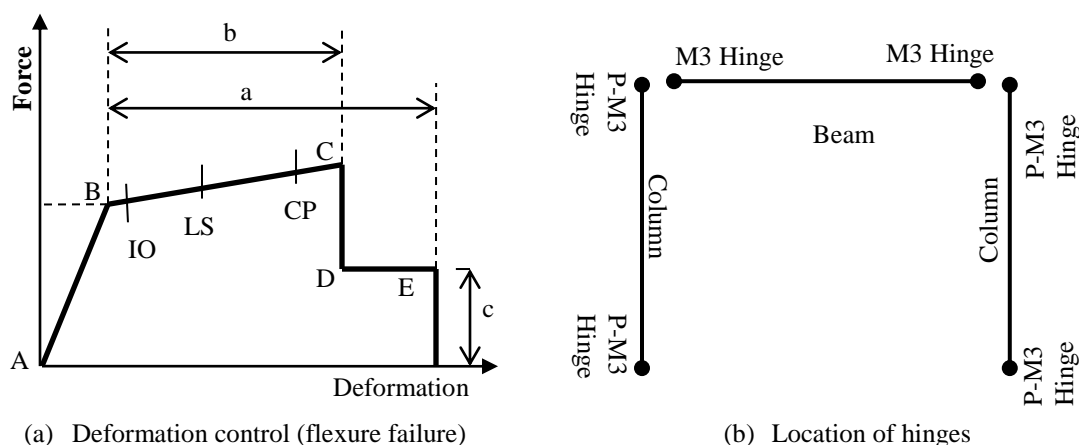


Fig. 5: Idealized inelastic force–deformation relationship

Table 5: Modelling parameters and numerical acceptability standards for RC beams

| Conditions | | | Modeling Parameters | | | Acceptance Criteria | | | | |
|-----------------------------------|---------------|-------------------------------|----------------------------------|------|-------------------------|----------------------------------|-------------------|-----------|------|------|
| $\frac{\rho - \rho'}{\rho_{bal}}$ | Trans. Reinf. | $\frac{V}{b_w d \sqrt{f'_c}}$ | Plastic rotation angle (radians) | | Residual strength ratio | Plastic rotation angle (radians) | | | | |
| | | | A | b | | c | Performance level | | | |
| | | | | | | IO | Component type | | | |
| | | | | | | | Primary | Secondary | | |
| | | | | | | | LS | CP | LS | CP |
| ≤ 0.0 | C | ≤ 3 | 0.025 | 0.05 | 0.2 | 0.010 | 0.020 | 0.025 | 0.02 | 0.05 |
| ≥ 0.5 | C | ≥ 3 | 0.020 | 0.03 | 0.2 | 0.005 | 0.010 | 0.02 | 0.02 | 0.03 |

Table 6: Modelling parameters and numerical acceptability standards for RC columns

| Conditions | | Modeling Parameters | | | | Acceptance Criteria | | | | |
|---------------------|---------------|------------------------------|----------------------------------|-------|-------------------------|---------------------|--|-------|-------|-------|
| $\frac{P}{A_g f_c}$ | Trans. Reinf. | $\frac{V}{b_w d \sqrt{f_c}}$ | Plastic rotation angle (radians) | | Residual strength ratio | IO | Plastic rotation angle (radians) Performance level | | | |
| | | | A | b | | | Component type | | LS | CP |
| ≤ 0.1 | C | ≤ 3 | 0.02 | 0.03 | 0.2 | 0.005 | 0.015 | 0.02 | 0.02 | 0.03 |
| ≥ 0.40 | C | ≥ 3 | 0.015 | 0.025 | 0.2 | 0.003 | 0.012 | 0.015 | 0.018 | 0.025 |

The responses of the example RCMRFs were studied with respect to fundamental period of vibration, roof displacement, base shear and story displacement. Using the empirical equation provided in IS 1893 for buildings without infills, the natural period of vibration was calculated. Table 3 provides the modal characteristics of each example RCMRFs.

Modal analysis of the example RCMRFs using Eigenvalues was carried out to find the fundamental period of vibration; the outcomes are shown in Table 3. The longest modal time period of vibration in the first mode is the fundamental period. The numbers that were determined utilizing code empirical relation and the basic period found using Eigenvalue analysis is virtually identical. The modal time period difference decreases as bay width increases. We can therefore draw the conclusion that the seismic code makes conservative design assumptions since it underestimates the natural duration of vibration.

Capacity curve, a plot between rooftop displacement and base shear, is used to represent the POA result. Table 7 displays base shear and rooftop displacement of example RCMRFs at the performance point for different load patterns. The engineering demand parameters, namely strength, stiffness, and ductility, generated from POA, are used in parametric to examine the seismic behavior of these RCMRFs. The pushover findings of the S8B3 RCMRF are extensively discussed for illustration purposes. The pushover curve of the S8B3 RCMRF is illustrated in Figure 6 for different loading patterns.

Table 7: Base shear and displacement of the example RCMRFs for different lateral load patterns

| Push Load Case | Group | Example RCMRFs | PBSE Procedures | | | | | | | |
|----------------|-------|----------------|-----------------|-------|----------------|-------|---------------|-------|----------------|-------|
| | | | ATC 40 (CSM) | | FEMA 440 (CSM) | | FEMA356 (DCM) | | FEMA 440 (DCM) | |
| | | | V | D | V | D | V | D | V | D |
| PUSH 1 | I | S3B1 | 175.14 | 0.021 | 201.98 | 0.03 | 196.50 | 0.026 | 202.62 | 0.038 |
| | | S6B1 | 131.81 | 0.09 | 142.23 | 0.109 | 142.43 | 0.133 | 142.61 | 0.203 |
| | | S9B1 | 92.24 | 0.164 | 93.72 | 0.173 | 99.76 | 0.211 | 107.31 | 0.262 |
| | | S12B1 | 74.17 | 0.236 | 73.82 | 0.229 | 78.28 | 0.315 | 78.28 | 0.315 |
| | | S15B1 | 57.20 | 0.317 | 55.60 | 0.267 | 59.57 | 0.403 | 59.57 | 0.403 |

| | | | | | | | | | | |
|-----------|-----|--------------|--------|-------|--------|-------|--------|-------|--------|-------|
| | II | S3B2 | 299.64 | 0.021 | 333.44 | 0.03 | 330.73 | 0.026 | 334.39 | 0.038 |
| | | S6B2 | 232.18 | 0.088 | 243.06 | 0.101 | 246.05 | 0.127 | 246.24 | 0.200 |
| | | S9B2 | 168.16 | 0.157 | 168.02 | 0.156 | 178.95 | 0.202 | 190.19 | 0.252 |
| | | S12B2 | 137.21 | 0.221 | 134.12 | 0.2 | 143.01 | 0.279 | 143.01 | 0.279 |
| | | S15B2 | 106.23 | 0.302 | 103.51 | 0.239 | 109.22 | 0.375 | 109.22 | 0.375 |
| | III | S3B3 | 419.99 | 0.021 | 460.93 | 0.03 | 460.22 | 0.026 | 462.20 | 0.037 |
| | | S6B3 | 332.31 | 0.087 | 343.33 | 0.097 | 347.24 | 0.126 | 347.46 | 0.197 |
| | | S9B3 | 244.17 | 0.154 | 243.12 | 0.151 | 257.89 | 0.198 | 272.90 | 0.247 |
| | | S12B3 | 198.92 | 0.217 | 193.29 | 0.19 | 208.03 | 0.256 | 208.03 | 0.265 |
| | | S15B3 | 155.36 | 0.297 | 151.63 | 0.228 | 158.59 | 0.358 | 158.59 | 0.358 |
| | IV | S3B4 | 546.21 | 0.021 | 596.14 | 0.03 | 595.31 | 0.026 | 597.84 | 0.037 |
| | | S6B4 | 433.84 | 0.087 | 449.25 | 0.097 | 452.01 | 0.124 | 452.94 | 0.195 |
| | | S9B4 | 320.23 | 0.153 | 318.34 | 0.148 | 336.49 | 0.195 | 355.17 | 0.244 |
| | | S12B4 | 260.37 | 0.215 | 252.36 | 0.184 | 270.27 | 0.255 | 270.27 | 0.255 |
| | | S15B4 | 204.44 | 0.294 | 199.76 | 0.222 | 207.95 | 0.349 | 207.94 | 0.349 |
| | V | S3B5 | 670.38 | 0.021 | 727.64 | 0.03 | 726.67 | 0.026 | 729.73 | 0.038 |
| | | S6B5 | 534.70 | 0.086 | 552.83 | 0.097 | 556.26 | 0.123 | 556.58 | 0.193 |
| | | S9B5 | 396.31 | 0.152 | 393.68 | 0.147 | 414.26 | 0.191 | 437.93 | 0.242 |
| | | S12B5 | 321.86 | 0.214 | 310.98 | 0.18 | 332.94 | 0.251 | 332.94 | 0.251 |
| | | S15B5 | 253.63 | 0.292 | 248.06 | 0.219 | 257.56 | 0.345 | 257.56 | 0.345 |
| PUSH 2 | I | S3B1 | 208.49 | 0.011 | 240.35 | 0.015 | 259.85 | 0.018 | 287.39 | 0.023 |
| | | S6B1 | 201.27 | 0.065 | 210.12 | 0.076 | 210.40 | 0.098 | 210.75 | 0.125 |
| | | S9B1 | 152.65 | 0.111 | 157.28 | 0.128 | 168.61 | 0.171 | 168.73 | 0.208 |
| | | S12B1 | 121.23 | 0.158 | 123.62 | 0.169 | 134.33 | 0.218 | 134.33 | 0.218 |
| | | S15B1 | 100.20 | 0.209 | 99.68 | 0.202 | 105.93 | 0.287 | 105.93 | 0.287 |
| | II | S3B2 | 368.04 | 0.012 | 418.56 | 0.016 | 443.23 | 0.018 | 467.85 | 0.023 |
| | | S6B2 | 357.47 | 0.063 | 360.05 | 0.07 | 360.50 | 0.094 | 360.52 | 0.12 |
| | | S9B2 | 275.42 | 0.106 | 286.22 | 0.122 | 298.86 | 0.161 | 297.83 | 0.197 |
| | | S12B2 | 218.35 | 0.153 | 218.52 | 0.153 | 236.19 | 0.206 | 246.34 | 0.239 |
| | | S15B2 | 183.69 | 0.202 | 180.58 | 0.183 | 191.84 | 0.272 | 191.84 | 0.272 |
| | III | S3B3 | 525.53 | 0.012 | 597.33 | 0.016 | 625.72 | 0.018 | 640.37 | 0.023 |
| | | S6B3 | 507.47 | 0.062 | 507.58 | 0.067 | 508.16 | 0.093 | 507.97 | 0.118 |
| | | S9B3 | 396.29 | 0.105 | 409.81 | 0.118 | 425.35 | 0.155 | 424.01 | 0.192 |
| | | S12B3 | 314.91 | 0.151 | 313.33 | 0.148 | 337.27 | 0.2 | 351.31 | 0.233 |
| | | S15B3 | 266.26 | 0.199 | 260.44 | 0.176 | 277.24 | 0.262 | 277.24 | 0.262 |
| | IV | S3B4 | 693.13 | 0.012 | 768.67 | 0.016 | 813.25 | 0.018 | 829.64 | 0.023 |
| | | S6B4 | 658.82 | 0.062 | 658.94 | 0.066 | 659.66 | 0.092 | 660.40 | 0.118 |
| | | S9B4 | 516.06 | 0.104 | 533.07 | 0.117 | 551.87 | 0.151 | 549.77 | 0.189 |
| | | S12B4 | 411.58 | 0.15 | 408.22 | 0.145 | 438.06 | 0.196 | 456.08 | 0.23 |

| | | | | | | | | | | |
|--------------|--------------|--------------|--------|--------|--------|--------|--------|--------|---------|-------|
| PUSH 3 | V | S15B4 | 348.41 | 0.198 | 340.50 | 0.173 | 362.48 | 0.254 | 362.48 | 0.254 |
| | | S3B5 | 854.16 | 0.012 | 946.60 | 0.016 | 998.74 | 0.019 | 1010.94 | 0.023 |
| | | S6B5 | 810.27 | 0.061 | 810.41 | 0.065 | 810.80 | 0.091 | 810.83 | 0.117 |
| | | S9B5 | 636.16 | 0.104 | 656.91 | 0.116 | 679.29 | 0.149 | 677.95 | 0.187 |
| | | S12B5 | 507.76 | 0.15 | 503.55 | 0.145 | 538.78 | 0.194 | 560.73 | 0.228 |
| | | S15B5 | 430.54 | 0.197 | 420.18 | 0.17 | 446.22 | 0.246 | 446.22 | 0.246 |
| | I | S3B1 | 179.19 | 0.018 | 213.66 | 0.025 | 208.47 | 0.024 | 216.73 | 0.034 |
| | | S6B1 | 146.44 | 0.083 | 155.80 | 0.099 | 156.06 | 0.126 | 156.21 | 0.186 |
| | | S9B1 | 103.99 | 0.15 | 106.60 | 0.164 | 113.45 | 0.203 | 121.15 | 0.25 |
| | | S12B1 | 82.97 | 0.216 | 83.34 | 0.219 | 87.25 | 0.28 | 87.25 | 0.28 |
| | | S15B1 | 62.63 | 0.298 | 61.18 | 0.257 | 66.52 | 0.38 | 65.52 | 0.38 |
| | II | S3B2 | 308.65 | 0.018 | 357.99 | 0.027 | 353.20 | 0.024 | 358.82 | 0.033 |
| | | S6B2 | 261.67 | 0.08 | 271.46 | 0.091 | 271.84 | 0.119 | 271.89 | 0.175 |
| | | S9B2 | 193.20 | 0.142 | 195.28 | 0.149 | 207.35 | 0.194 | 218.18 | 0.237 |
| | | S12B2 | 152.82 | 0.203 | 150.56 | 0.192 | 161.98 | 0.255 | 161.98 | 0.255 |
| | | S15B2 | 117.90 | 0.282 | 115.14 | 0.228 | 121.17 | 0.351 | 121.17 | 0.351 |
| | III | S3B3 | 439.15 | 0.018 | 497.26 | 0.026 | 496.73 | 0.024 | 498.56 | 0.033 |
| | | S6B3 | 377.38 | 0.079 | 384.98 | 0.087 | 385.09 | 0.118 | 385.32 | 0.172 |
| | | S9B3 | 282.49 | 0.139 | 284.68 | 0.145 | 300.50 | 0.188 | 315.09 | 0.233 |
| | | S12B3 | 222.39 | 0.199 | 217.45 | 0.182 | 233.96 | 0.245 | 233.96 | 0.245 |
| | | S15B3 | 173.40 | 0.276 | 169.26 | 0.217 | 177.00 | 0.336 | 177.00 | 0.336 |
| | IV | S3B4 | 570.56 | 0.018 | 643.95 | 0.026 | 643.39 | 0.024 | 645.59 | 0.033 |
| | | S6B4 | 494.26 | 0.079 | 502.45 | 0.087 | 502.60 | 0.117 | 502.88 | 0.17 |
| | | S9B4 | 371.92 | 0.137 | 373.95 | 0.141 | 392.61 | 0.183 | 408.30 | 0.229 |
| | | S12B4 | 291.63 | 0.197 | 284.27 | 0.177 | 304.60 | 0.236 | 304.60 | 0.236 |
| S15B4 | | 228.93 | 0.273 | 223.42 | 0.211 | 232.81 | 0.327 | 232.81 | 0.327 | |
| V | S3B5 | 701.79 | 0.018 | 786.77 | 0.026 | 786.14 | 0.024 | 788.78 | 0.033 | |
| | S6B5 | 610.81 | 0.079 | 617.63 | 0.085 | 617.74 | 0.116 | 618.13 | 0.169 | |
| | S9B5 | 460.73 | 0.131 | 459.96 | 0.12 | 463.54 | 0.168 | 466.89 | 0.212 | |
| | S12B5 | 360.79 | 0.196 | 351.18 | 0.174 | 375.33 | 0.231 | 375.33 | 0.231 | |
| | S15B5 | 284.29 | 0.271 | 277.51 | 0.208 | 288.40 | 0.319 | 288.40 | 0.319 | |

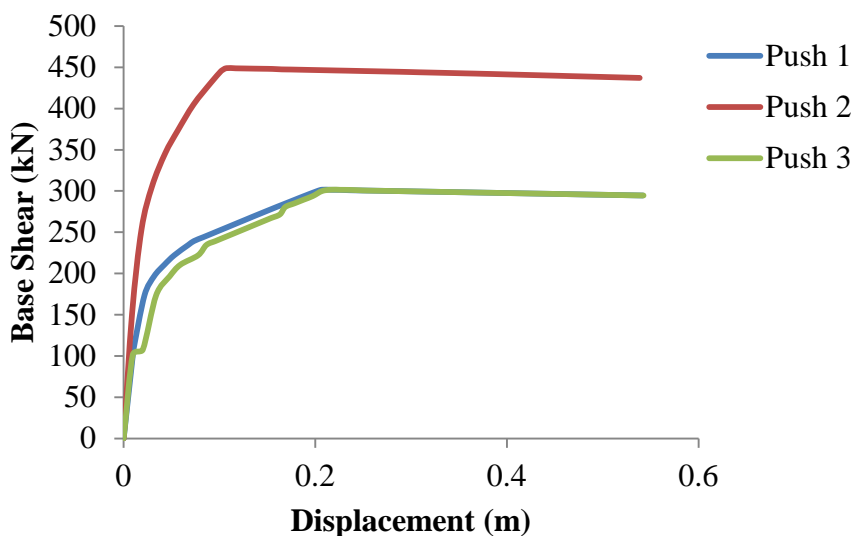
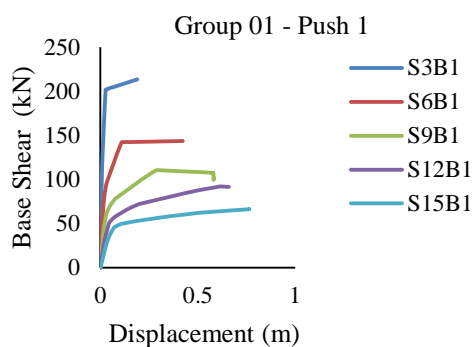


Fig. 6: Pushover curve of S8B3 RCMRF for three distinct lateral load patterns

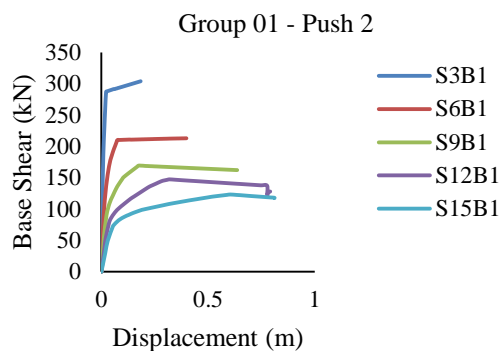
The base shear and displacement at performance point serve to describe the nonlinear properties of the example RCMRFs. According to the analysis of the S8B3 capacity curve, the Push 2 load case demonstrated a force-controlled mechanism, while the Push 1 load case described a displacement-controlled system. Therefore, a set of lateral loads must be applied to evaluate the effects of lateral loads on an example RCMRF. Table 8 provides the base shear and displacement at a performance point for example S8B3 RCMRF. Pushover curve of all example RCMRFs is shown in Figure 7 (a) – (o).

Table 8: Values of base shear and displacement at performance point of example S8B3 RCMRF

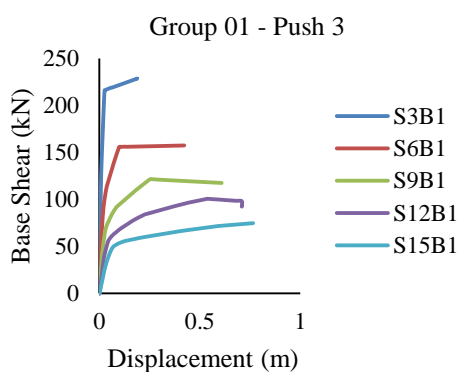
| Example RCMRF S8B3 | ATC 40 (CSM) | | FEMA 440 (CSM) | | FEMA 356 (DCM) | | FEMA 440 (DCM) | |
|--------------------|--------------|-------|----------------|-------|----------------|-------|----------------|-------|
| | V | D | V | D | V | D | V | D |
| Push 1 | 267.17 | 0.131 | 268.79 | 0.135 | 286.92 | 0.173 | 301.38 | 0.225 |
| Push 2 | 430.33 | 0.09 | 447.01 | 0.104 | 448.35 | 0.14 | 446.90 | 0.192 |
| Push 3 | 308.61 | 0.118 | 313.77 | 0.128 | 334.04 | 0.166 | 334.67 | 0.21 |



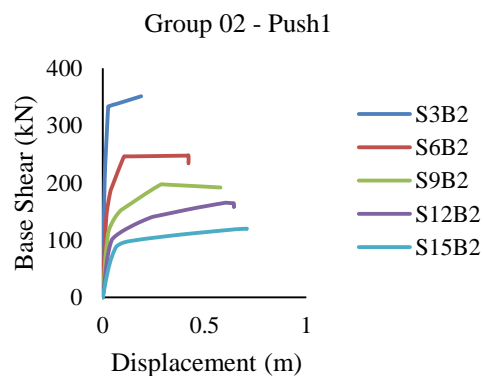
(a) Pushover Curve Of Group I RCMRFs



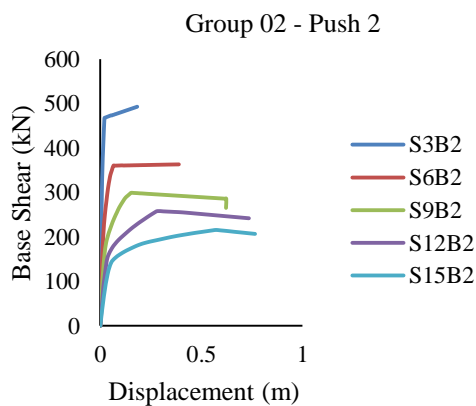
(b) Pushover Curve Of Group I RCMRFs



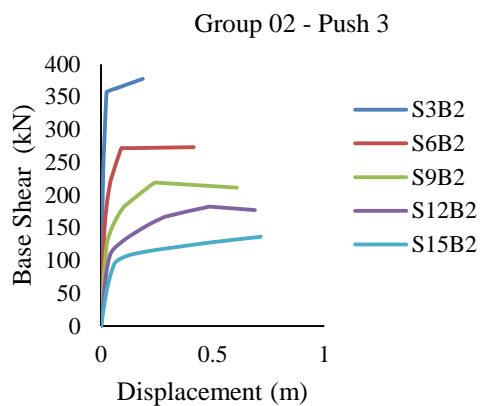
(c) Pushover Curve Of Group I RCMRFs



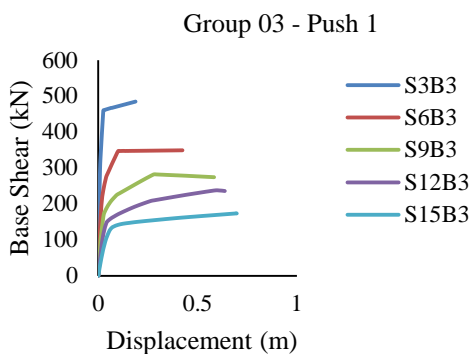
(d) Pushover Curve Of Group II RCMRFs



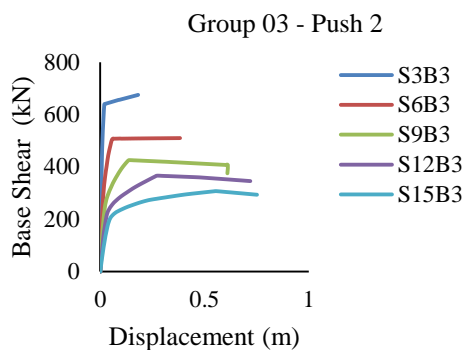
(e) Pushover Curve Of Group II RCMRFs



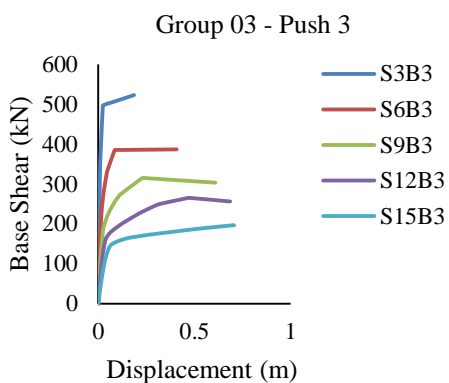
(f) Pushover Curve Of Group II RCMRFs



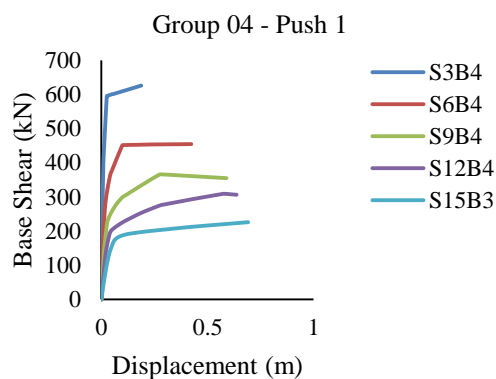
(g) Pushover Curve Of Group III RCMRFs



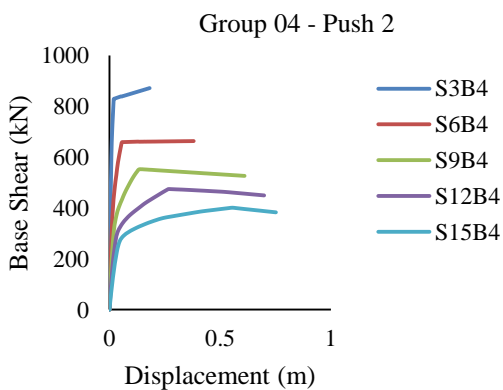
(h) Pushover Curve Of Group III RCMRFs



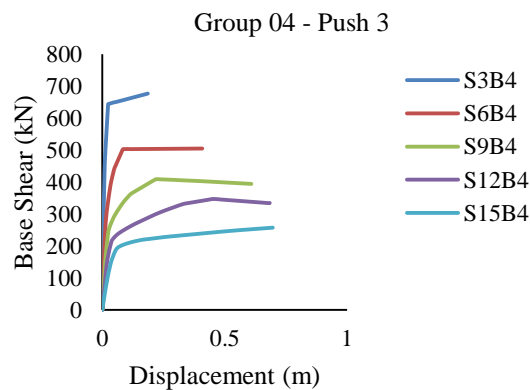
(i) Pushover Curve Of Group III RCMRFs



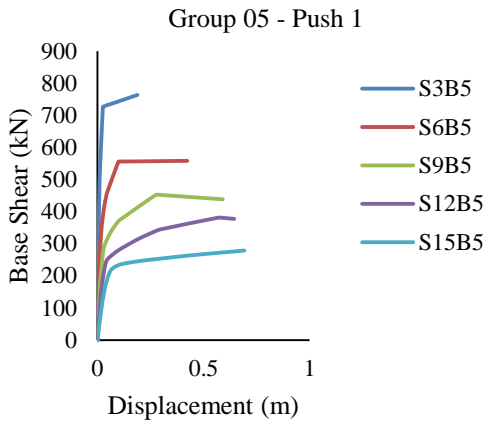
(j) Pushover Curve Of Group IV RCMRFs



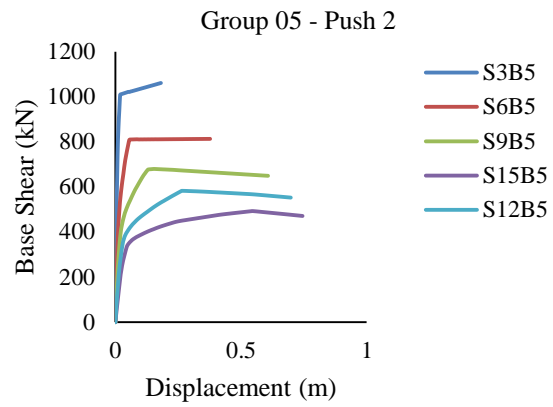
(k) Pushover Curve Of Group IV RCMRFs



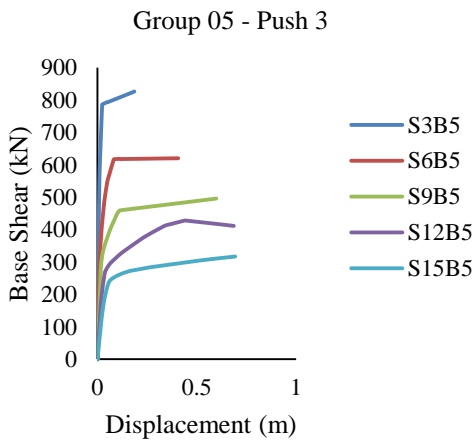
(l) Pushover Curve Of Group V RCMRFs



(m) Pushover Curve Of Group V RCMRFs



(n) Pushover Curve Of Group V RCMRFs



(o) Pushover Curve Of Group V RCMRFs

Fig. 7: Pushover curve of all example RCMRFs for three distinct lateral load patterns

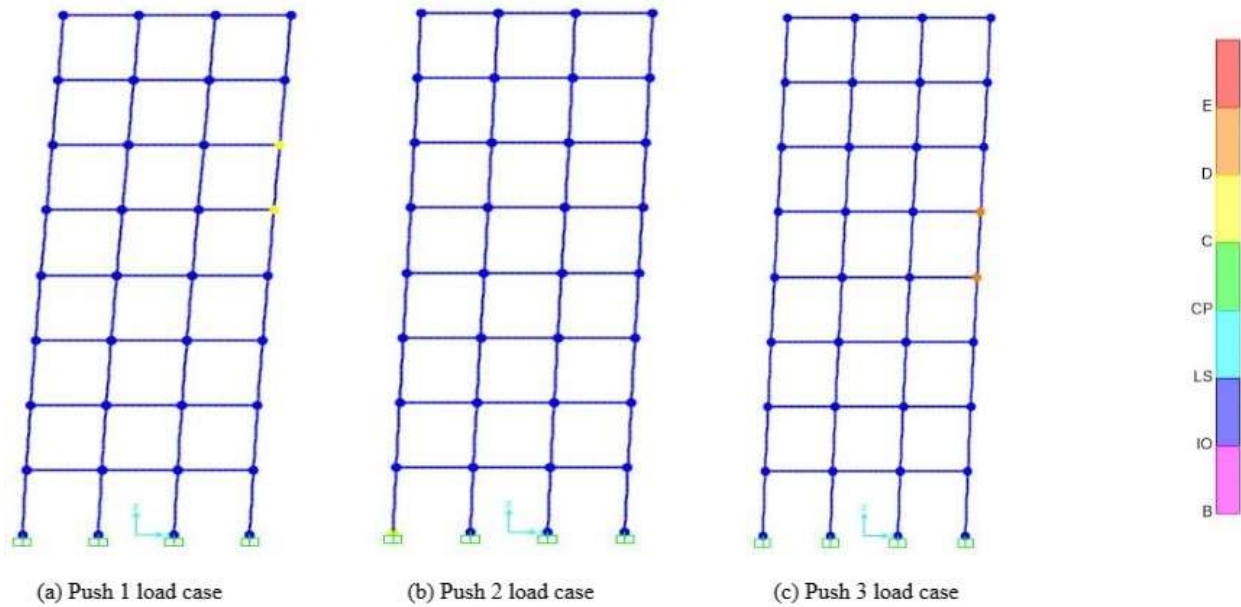


Fig. 8: Collapse Mechanism of the plastic hinges in Example S8B3 RCMRF

The initial slopes of the capacity curve describe the structural components of the RCMRF that have been damaged. The RCMRF initial slope in the load case Push 2 for S8B3 is higher than that in the load case Push 1.

This might be a result of plastic hinges yield mechanism. In the load case Push 2, damages concentrate in the upper storeys (in the beams only) for larger values of displacement, whereas in the load case Push 1, damages are concentrated in the lower storeys (in the columns). Consequently, it can be said that push 1's load case is force-controlled. Figure 8 describes the collapse mechanism of S8B3 RCMRF. Table 9 gives initial stiffness of S8B3 RCMRF subjected to different loading condition.

In PBSD performance of a structure is defined by discrete levels namely Operation level (OP), Immediate Occupancy (IO), Life Safety range (LS), Collapse Prevention level (CP) and Collapse (C). These are identified based on damages to structural and non-structural components. Table 10 shows the permissible limits of drift and obtained drift of S8B3 RCMRF.

Table 9: Values of initial stiffness for example S8B3 RCMRF for different load patterns

| Example S8B3 RCMRF | Initial Stiffness (kN/m) |
|--------------------|--------------------------|
| PUSH 01 | 10571.6 |
| PUSH 02 | 17252.9 |
| PUSH 03 | 12134.5 |

Table 10: Permissible limits of drift and obtained drift of S8B3 RCMRF

| Performance levels | Drift Value |
|--------------------|-------------|
|--------------------|-------------|

| | Prescribed value (%) | Obtained value (%) | | |
|---------------------------|----------------------|--------------------|--------|--------|
| | | Push 1 | Push 2 | Push 3 |
| Operational level | < 0.7 | 0.040 | 0.036 | 0.039 |
| Immediate occupancy level | 1 | 0.042 | 0.036 | 0.039 |
| Life safety level | 2 | 0.784 | 0.886 | 0.822 |
| Collapse prevention level | 4 | 2.256 | 2.243 | 2.300 |
| Collapse | > 4 | 2.256 | 2.243 | 2.300 |

In POA lateral loads are applied incrementally, in each incremental step of POA there is increase in lateral drift. The attainment of a damage state is identified by the permissible limits of drift as described in FEMA. Table 10 provides the details of drift of S8B3 RCMRF at identified performance levels. These performance levels have been traced with reference to formation of plastic hinges (both in beams and columns) and their transition from one performance level to other.

The formation of first hinge is considered to be attainment of operational level (OP). later sequence of shift of this plastic hinge are used to accumulate the responses in other performance levels. It has been observed that during a POA there is a fall in strength and stiffness at each incremental step. Table 11 provides the displacement, base shear and stiffness at identified performance levels of S8B3 RCMRF.

Table 11: Displacement, Base shear and Stiffness at identified performance level of S8B3 MRF

| Performance levels | Push 1 | | | Push 2 | | | Push 3 | | |
|---------------------------|------------------|-----------------|------------------|------------------|-----------------|------------------|------------------|-----------------|------------------|
| | Displacement (m) | Base Shear (kN) | Stiffness (kN/m) | Displacement (m) | Base Shear (kN) | Stiffness (kN/m) | Displacement (m) | Base Shear (kN) | Stiffness (kN/m) |
| Operational level | 0.01 | 101.49 | 10571.56 | 0.01 | 151.36 | 17252.94 | 0.01 | 115.22 | 12134.49 |
| Immediate occupancy level | 0.01 | 107.62 | 10571.61 | 0.01 | 151.36 | 17252.94 | 0.01 | 115.22 | 12134.49 |
| Life safety level | 0.19 | 293.92 | 1561.01 | 0.21 | 446.41 | 2098.62 | 0.20 | 334.86 | 1696.55 |
| Collapse prevention level | 0.54 | 294.59 | 543.99 | 0.54 | 437.16 | 811.97 | 0.55 | 327.52 | 593.35 |
| Collapse | 0.54 | 294.59 | 543.99 | 0.54 | 437.16 | 811.97 | 0.55 | 327.52 | 593.35 |

PBSE procedures are useful to identify the collapse mechanism through the formation of plastic hinges. One can attempt to scale the damage state of the structure using this collapse mechanism. The engineering demand parameters such as storey drift, inter-storey drift, base shear and derived quantities such as ductility, stiffness and energy dissipated can be used to form a damage indicator.

Many attempts have been made in past to scale these damages. The document damage indicators in available literature as calibrated using nonlinear dynamic analysis. These efforts have result in affirmative way of damage assessment but follows the limitation computational effort, hence not found common in practice. Some researchers have provided damage assessment indices using nonlinear static methods but followed the limitation of POA to address the inelastic

excursion. This demand a rational approach of damage assessment integrated with PBSE which will help designer to identify attainment of performance level with a damage value. Such an attempt will help designers to follow the frameworks of next-generation PBSD with identified performance levels in terms of repair, downtime and casualties. The scope of the present study is to understand the available PBSE procedures and identify the gray areas towards integration of PBSE with damage assessment.

Conclusion:

Studies have been done on various performance-based seismic evaluation techniques that are listed in PBSD. For this, 75 force-based design RCMRFs were put under various lateral loads, and a parametric research was conducted to investigate the performance levels of the buildings. The chosen frames show how low-rise, medium-rise, and high-rise building designs and construction techniques are generally applied throughout the Indian subcontinent.

The arrangement of the sample RCMRFs used to demonstrate these consequences of an increase in storey height and bay width. A recognized class of structures is represented by the groupings of example RCMRFs. Understanding the local and global behavior of example RCMRFs exposed to pre-defined seismic risks is made easier by the use of PBSE methods on the example RCMRFs. In order to determine the envelope of top bound and lower bound values of inelastic intrusions, various lateral load patterns were applied to example RCMRFs.

These envelopes were useful for figuring out the causes of failure. The parametric research done on the example RCMRFs demonstrated the potential of merging the PBSE with the attainment of a damage value that is required in order for the PBSD to become a standard procedure in practice. The following are the conclusions from the parametric study:

- The response reduction factors for forces and displacements are used to account for inelastic effects according to current seismic design rules. However, such a deceptive strategy makes it difficult to comprehend the true building performance in a nonlinear state.
- Current seismic codes' equivalent static technique for earthquake-resistant design is insufficient to account for higher modes of vibration, leading to cautious design.
- The capacity spectrum method and displacement coefficient method are the PBSE techniques recommended in PBSD. Which approach should be utilized in practice is an issue that is raised when these methods are evaluated for the example RCMRFs and reveal various results for displacements.
- Different lateral load patterns, including the trivial lateral load pattern proposed in IS 1893, the uniformly distributed lateral load pattern, and the elastic first mode lateral load pattern, were used in POA. The envelopes of upper and lower bound values are the outcome of these lateral load patterns. As a result, a single set of lateral load patterns cannot address nonlinear behavior; but, a set of two or more lateral load patterns can examine nonlinear phenomena in greater detail.

- The collapse mechanism caused by the PBSE methods illustrates how plastic hinges form and drop from one performance level to another. These mechanisms, namely force-controlled and displacement-controlled hinges, aid in determining the type of failure based on the concentration of hinges. The positioning and modelling of plastic hinges affect the collapse mechanism. It is necessary to optimize the modelling of nonlinear hinges and their placement in order to determine the precise values of nonlinear state.
- RCMRFs exhibit a force-controlled behavior when a uniform lateral load pattern is applied. This might be caused by the columns' development of hinges for shear and bending. However, for trivial load patterns, the displacement-controlled behavior manifests because only the bending of the beams causes the formation of plastic hinges.
- The stiffness value significantly decreases during the incremental POA steps, and PBSE has utilized this to track the achievement of various performance levels. The drift criterion served as the foundation for performance levels. They can only show when a certain limit state has been reached; they cannot scale any damage values.
- The assessment of building performance levels and the likelihood of damage is required by contemporary seismic design trends. These performance levels are currently a subject of inquiry.
- Significant work has been done in the current literature to integrate the damage state with the identified performance levels. These initiatives make use of nonlinear dynamic analysis, which requires laborious and complicated computations and is therefore not frequently used by professional engineers.
- Nonlinear static analysis has been attempted to assess the damage condition, but these efforts were constrained by the POA.

The current work focuses on overcoming POA's limitations to improve damage assessment processes utilizing POA. The engineering demand parameters that resulting from POA can be used to define the damage and vulnerability indicators. The scope currently only includes parametric studies of the engineering demand parameter. Future work will include calibrating the damage or vulnerability index.

Acknowledgement

The authors of this study recognize the research contributions made by all the cited sources as well as the assistance of MGM College of engineering, Nanded, India and by the Chairman, Kalinga University, New Raipur, Chhattisgarh, India.

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